

PART : PHYSICS

1. A solid sphere and a hollow sphere are roll down purely equal distances on same inclined plane (starting from rest) in time t_1 and t_2 then

(1) $t_1 > t_2$

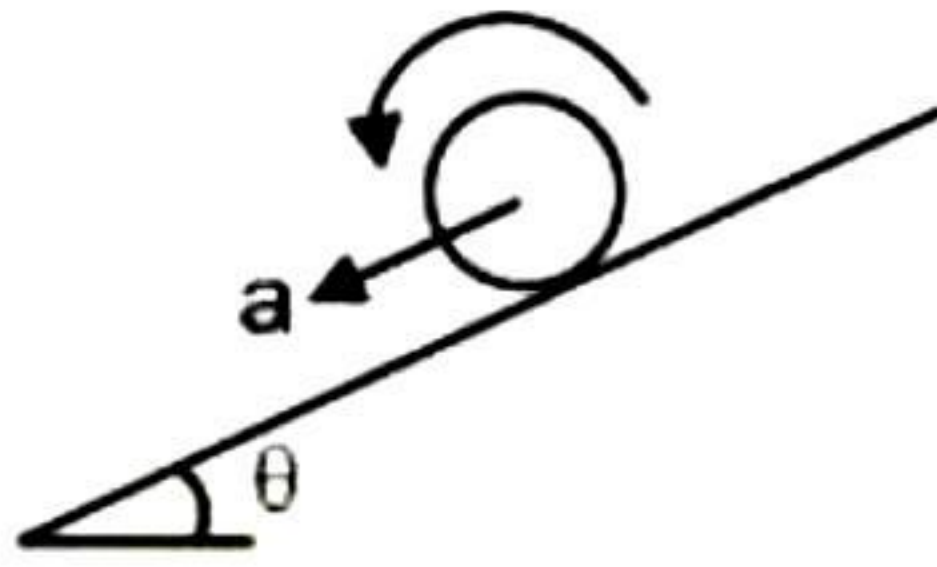
(2) $t_1 < t_2$

(3) $t_1 = 2t_2$

(4) $t_1 = t_2$

Ans. (2)

Sol.



$$a = \frac{g \sin \theta}{1 + \frac{I_{cm}}{mr^2}}$$

$$(I_{cm})_{solid} < (I_{cm})_{hollow}$$

$$a_{solid} > a_{hollow}$$

$$t_1 < t_2$$

2. A solid sphere rolls without slipping on a horizontal plane. What is ratio of translation kinetic energy to the rotation kinetic energy of the sphere?

(1) $4/3$

(2) $3/4$

(3) $2/5$

(4) $5/2$

Ans. (4)

Sol. $V = R\omega$

$$\frac{K_t}{K_{rot}} = \frac{\frac{1}{2}mv^2}{\frac{1}{2}I\omega^2} = \frac{\frac{1}{2}mv^2}{\frac{1}{2} \times \frac{2}{5}mv^2} = \frac{5}{2}$$

3. Acceleration due to gravity on the surface of earth is g and acceleration due to gravity on a planet whose diameter is $\frac{1}{3}$ of that of earth and same mass as that of earth is g' . If $g' = ng$ then n is.

(1) 9

(2) 2

(3) $\frac{1}{2}$

(4) 6

Ans. (1)

Sol. $g = \frac{GM}{R^2}$

$$g' = \frac{GM}{\left(\frac{R}{3}\right)^2} = \frac{9GM}{R^2}$$

$$g' = 9g$$

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4. If an object of rest mass M_0 has momentum p and total energy E then which the of the following will be correct ? (where C is the velocity of light) -

(1) $E^2 = M_0^2 C^2 + P^2 C^2$

(2) $E^2 = M_0^2 C^4 + P^2 C^2$

(3) $E = M_0 C^2 + PC^2$

(4) $E^2 = M_0 C + PC$

Ans. (2)

Sol. In relativistic case $m = \frac{m_0}{\sqrt{1 - \frac{v^2}{c^2}}}$

$$P^2 = \frac{m_0^2 v^2}{\left(1 - \frac{v^2}{c^2}\right)} = \frac{m_0^2 \frac{v^2}{c^2} c^2}{\left(1 - \frac{v^2}{c^2}\right)}$$

$$P^2 = \frac{m_0^2 c^2 \left(\frac{v^2}{c^2} - 1 + 1\right)}{\left(1 - \frac{v^2}{c^2}\right)}$$

$$P^2 = m_0^2 c^2 + \frac{m_0^2 c^2}{\left(1 - \frac{v^2}{c^2}\right)}$$

$$p^2 c^2 = m_0^2 c^2 + \left(\frac{m_0}{\sqrt{1 - \frac{v^2}{c^2}}}\right)^2 c^4$$

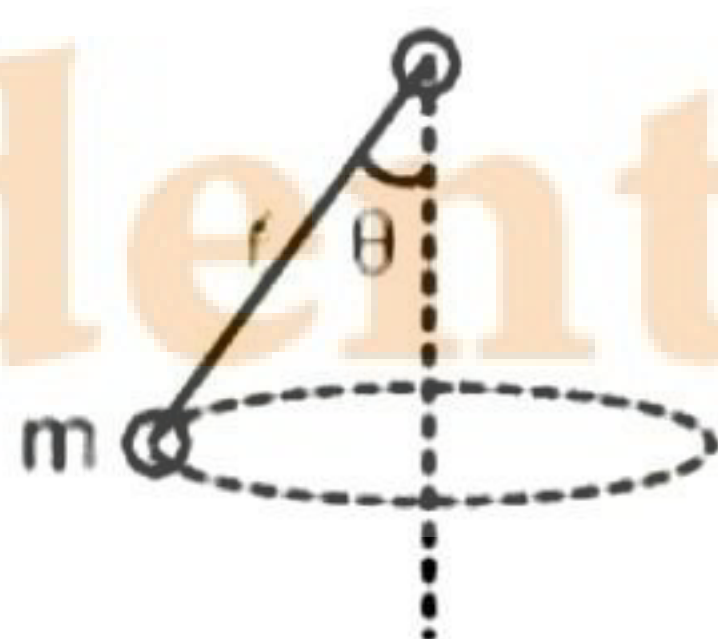
$$p^2 c^2 = -(m_0 c^2)^2 + (mc^2)^2$$

$$(mc^2)^2 = p^2 c^2 + (m_0 c^2)^2$$

$$E^2 = p^2 c^2 + m_0^2 c^4$$

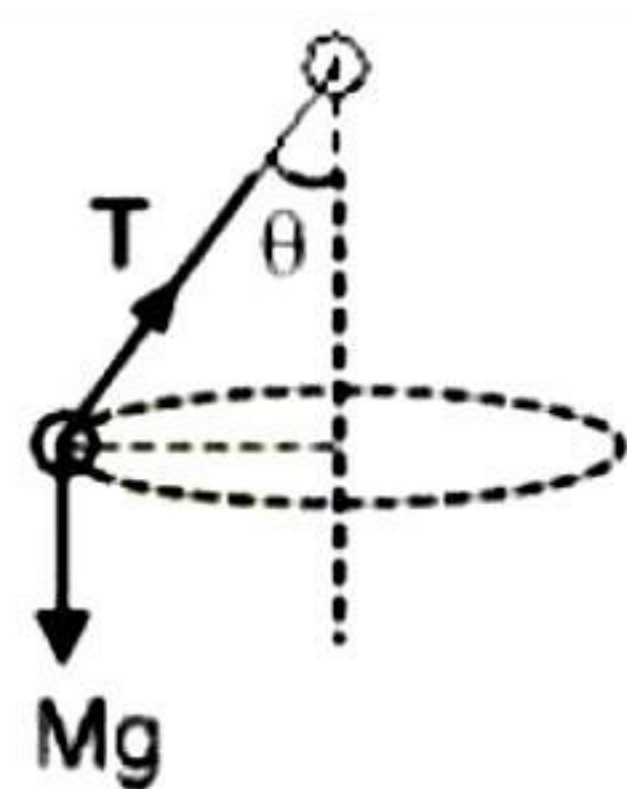
$$E = \sqrt{(pc)^2 + (m_0 c^2)^2}$$

5. A bob of mass m is attached to a string of length ' ℓ '. If it is rotating in a horizontal circle of radius r with angular velocity $\omega = \frac{3 \text{ rev}}{\pi \text{ sec}}$ and tension in the string is $x(m\ell)$ then value of x is _____



Ans. 36.00

Sol.



$$\omega = \frac{3 \text{ rev}}{\pi \text{ sec}}$$

$$\omega = \frac{3}{\pi} \times 2\pi \frac{\text{rev}}{\text{sec}}$$

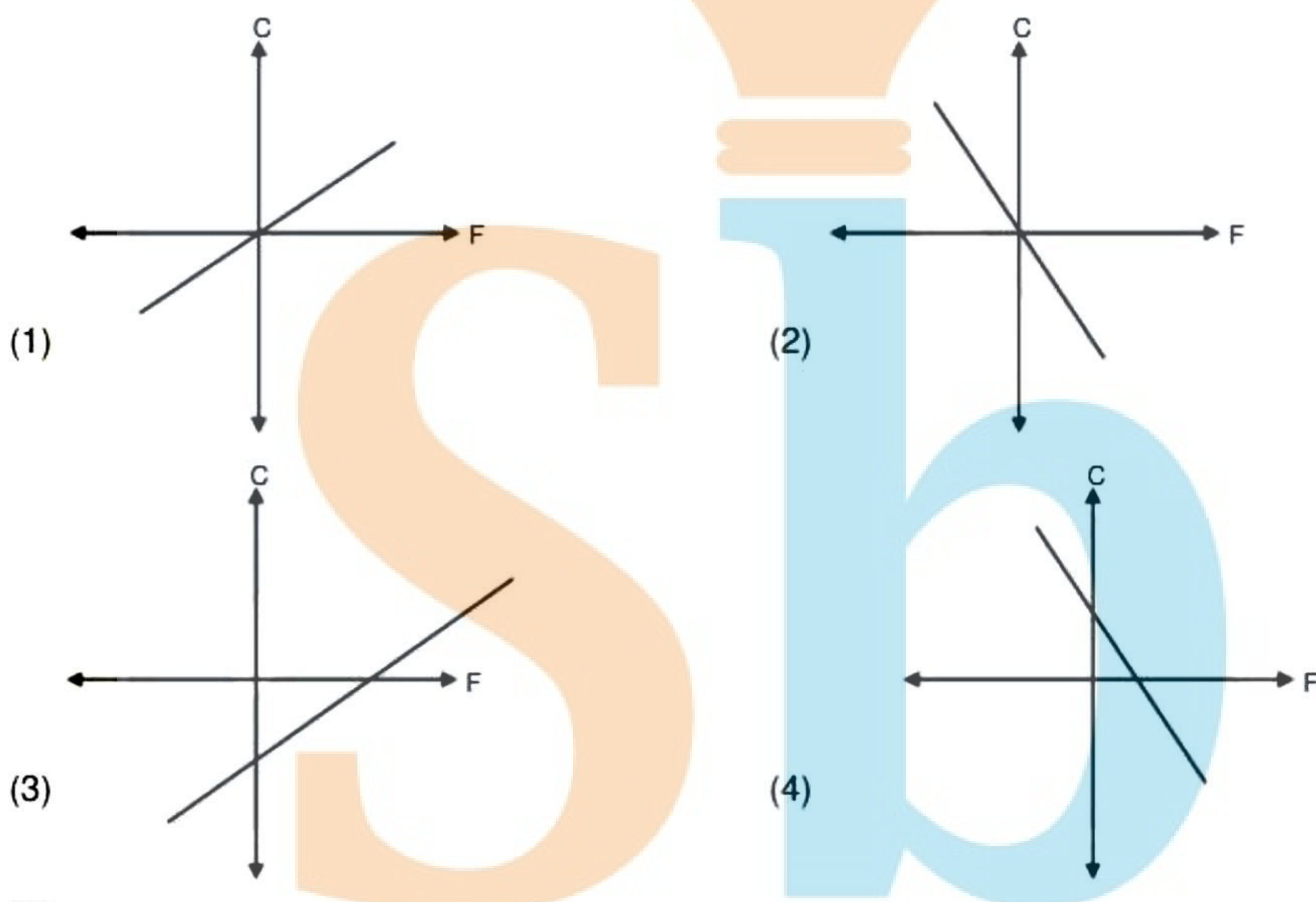
$$\omega = 6$$

$$T \sin \theta = m(\ell \sin \theta) \omega^2$$

$$T = m \omega^2 \ell = m(36) \ell = x(m \ell)$$

$$x = 36$$

6. Which of the following graph is correct. Hence F = Fahrenheit. & C = Celsius



Ans. (3)

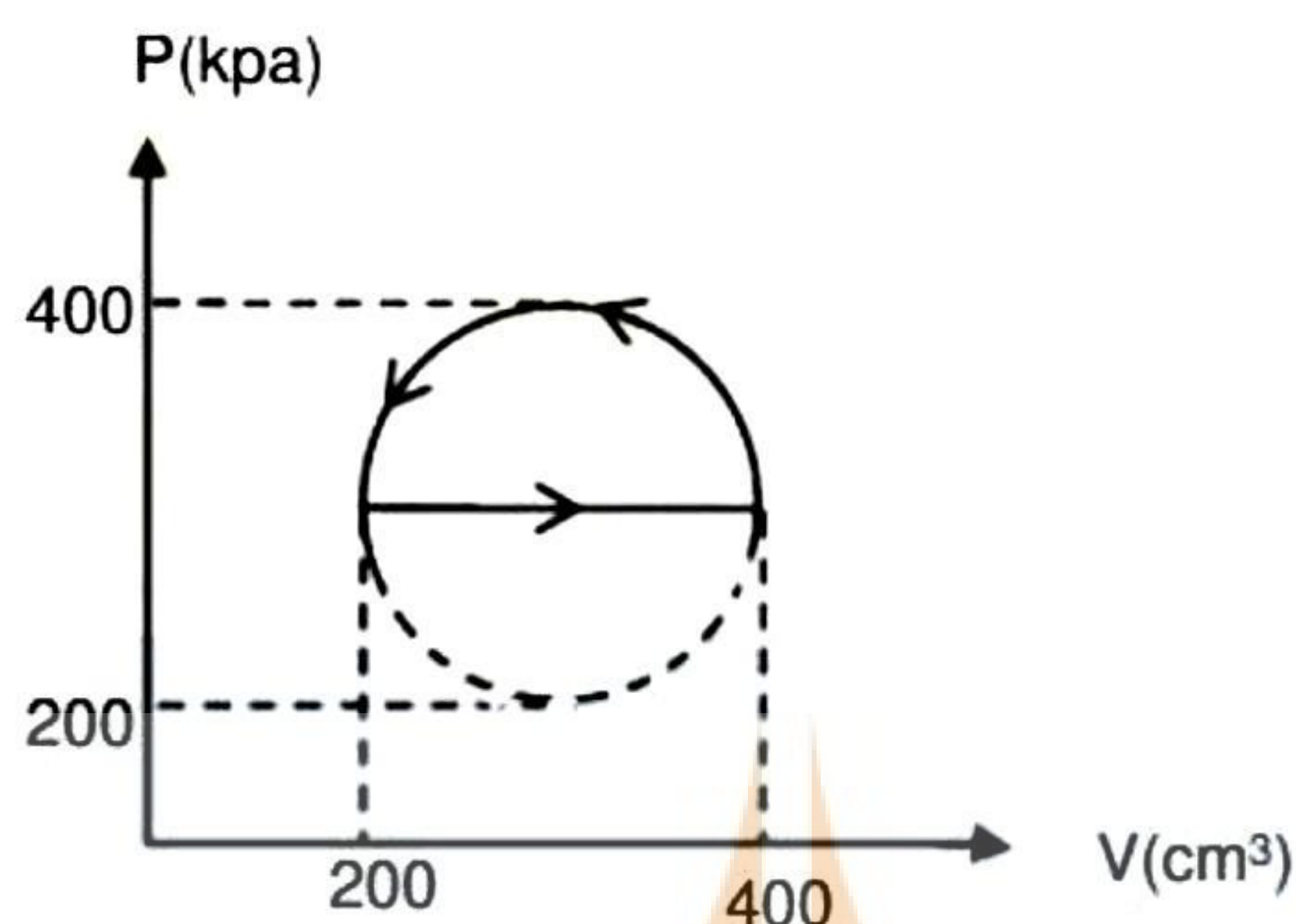
Sol. $\frac{C - 0}{100} = \frac{F - 32}{180} \Rightarrow C = \frac{5}{9}(F - 32)$

$$C = \frac{5F}{9} - \frac{160}{9}$$

$$\text{Slope} = \frac{5}{9} = +\text{Ve}$$

$$\text{Intercept} = \frac{-160}{9}$$

7. An ideal gas is undergone through a cyclic process as shown in the graph. The net heat ejected by the gas during one cycle will be :-



- (1) $5\pi\text{J}$ (2) $10\pi\text{J}$ (3) $15\pi\text{J}$ (4) $2.5\pi\text{J}$

Ans. (1)

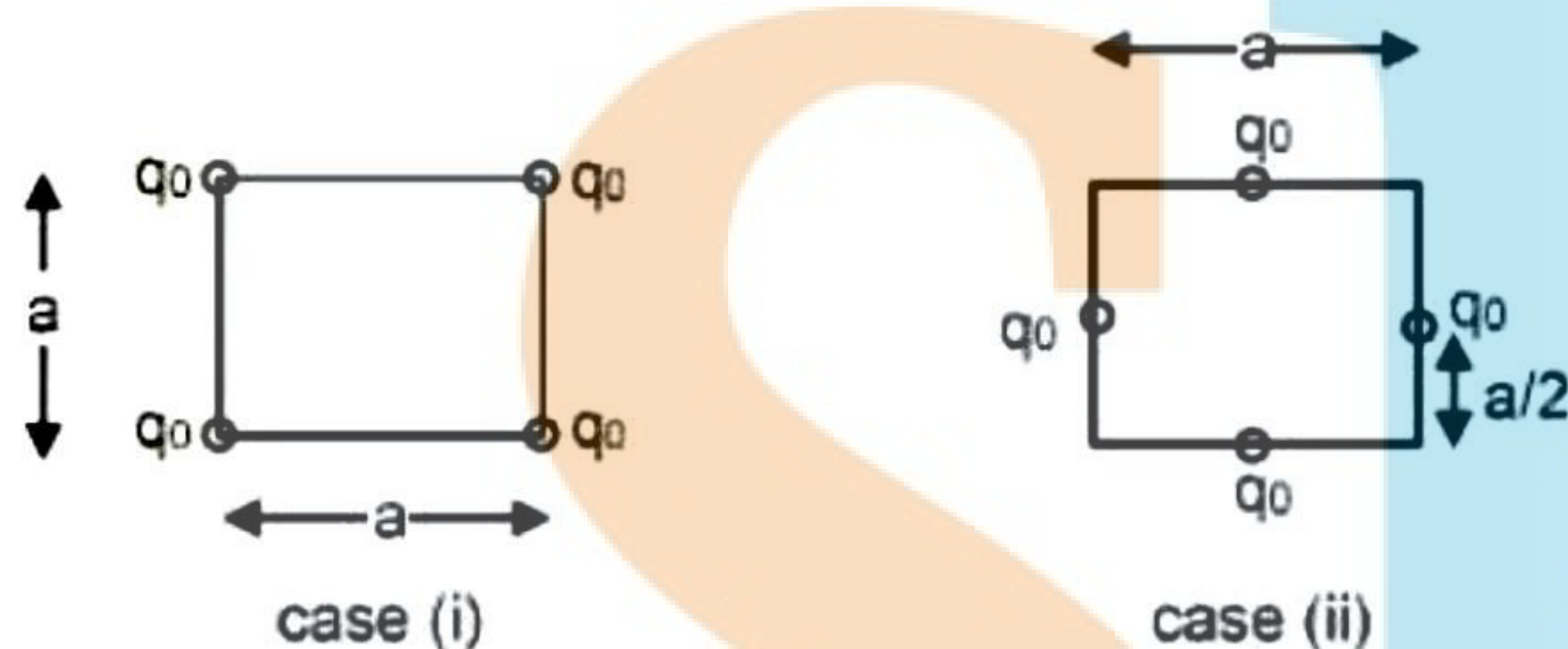
Sol. $W_{\text{cycle}} = \text{Area enclosed by P - V cycle} = \frac{\pi ab}{2}$

$$W_{\text{cycle}} = -\frac{1}{2} \pi (100 \times (10^{-2})^3) (100 \times 10^3)$$

$$Q_{\text{cycle}} = W_{\text{cycle}} = -5\pi$$

Heat rejected by the gas = $5\pi\text{J}$

8.



Four charges each of value q_0 are placed as shown. If potential energy of system is k_1 in case (i) and PE of system is k_2 in case (ii) then what is value of $k_2 - k_1$

- (1) $\frac{kq_0^2}{a} [3\sqrt{2} - 2]$ (2) $\frac{kq_0^2}{a} [5\sqrt{2} - 2]$ (3) $\frac{kq_0^2}{a} [3\sqrt{2} + 2]$ (4) Zero

Ans. (1)

Sol. $k_1 = 2 \left[\frac{kq_0^2}{a} + \frac{kq_0^2}{a} + \frac{kq_0^2}{\sqrt{2}a} \right] = \frac{2kq_0^2}{a} \left[2 + \frac{1}{\sqrt{2}} \right]$

$$k_2 = 2 \left[\frac{kq_0^2}{a/\sqrt{2}} \times 2 + \frac{kq_0^2}{a} \right] = \frac{2kq_0^2}{a} [2\sqrt{2} + 1]$$

$$k_2 - k_1 = \frac{kq_0^2}{a} (3\sqrt{2} - 2)$$

9. **Statement-1:** If in adiabatic process volume is decrease from V to $V/2$ then temperature also decreases
Statement-2: Free expansion is irreversible as well as adiabatic
 (1) Statement-1 is True, Statement-2 is True; Statement-2 is a correct explanation for Statement-1.
 (2) Statement-1 is True, Statement-2 is True; Statement-2 is NOT a correct explanation for Statement-1
 (3) Statement-1 is True, Statement-2 is False
 (4) Statement-1 is False, Statement-2 is True

Ans. (4)

Sol. $T.V^{\gamma-1} = \text{constant}$
 when volume decreases then temperature increases

10. Which of the following option is correct for increasing order of wave length

(i) Infrared ray

(ii) x-ray

(iii) UV-ray

(iv) Microwave-ray

(1) (i), (ii), (iii), (iv) (2) (iv), (i), (iii), (ii) (3) (ii), (iii), (i), (iv) (4) (ii), (iii), (i), (iv)

Ans. (3)

Sol. $\lambda_x < \lambda_{UV} < \lambda_{Ir} < \lambda_{Micro}$

11. Find the fringe width, if complete YDSE is immersed in a medium of refractive index $\mu = 1.44$.

Given $\lambda_{air} = 690 \text{ nm}$, $D = 0.72 \text{ meter}$ $d = 1.5 \text{ mm}$

(1) 0.23 mm (2) 1.23 mm (3) 2.28 mm (4) 0.40 mm

Ans. (1)

Sol. $\beta_{red} = \frac{\lambda_{air}}{\mu} \frac{D}{d}$

$$= \frac{690 \times 10^{-9} \times 72 \times 10^{-2}}{144 \times 10}$$

$$= \frac{690}{2 \times 3 \times 10^{-3}}$$

$$= 230 \times 10^{-6}$$

 0.23 mm

12. For which of the following inputs, the output will be zero (0) :-



(A) $x = 0, y = 0$

(B) $x = 0, y = 1$

(C) $x = 1, y = 0$

(D) $x = 1, y = 1$

(1) A,B,C

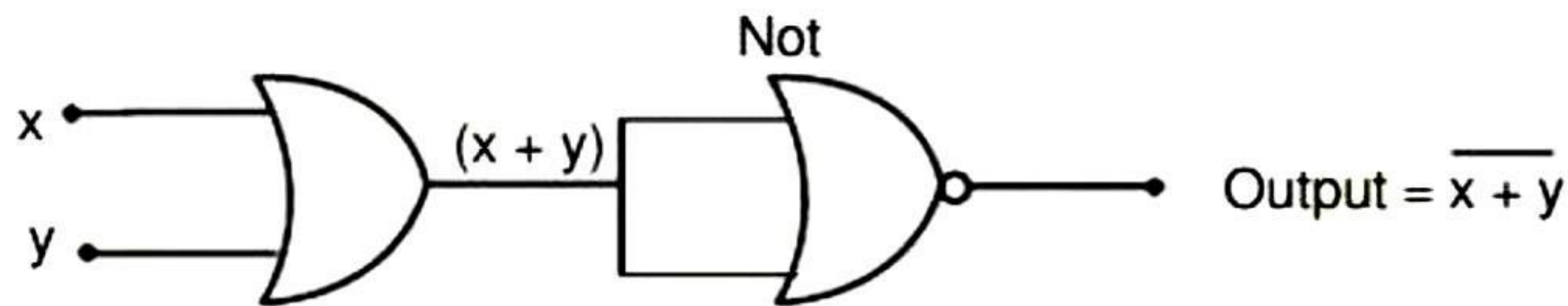
(2) B, C, D

(3) Only A

(4) Only D

Ans. (2)

Sol.



- (A) $x = 0, y = 0 \Rightarrow \text{output} = 0 + 0 = 1$
(B) $x = 0, y = 1 \Rightarrow \text{output} = 0 + 1 = 0$
(C) $x = 1, y = 0 \Rightarrow \text{output} = 1 + 0 = 0$
(D) $x = 1, y = 1 \Rightarrow \text{output} = 1 + 1 = 0$

13. Power of two sources S_1 and S_2 are in ratio 2 : 1 and 2×10^{15} photons per sec of wavelength 600 nm from S_1 are emitted then find the number of photons per second emitted from source S_2 of wavelength 300 nm ?

- (1) 5×10^{15} (2) 2×10^{15} (3) 5×10^{14} (4) 2×10^{14}

Ans. (3)

Sol. $P_1 = P = \frac{N_1 hc}{\lambda_1}$ $P = \frac{N_2 hc}{\lambda_2}$ $N \rightarrow \text{No. of photon/sec}$

$$P_2 = \frac{P}{2} = \frac{N_2 hc}{\lambda_2}$$

$$\frac{P_1}{P_2} = \frac{N_1}{N_2} \cdot \frac{\lambda_2}{\lambda_1}$$

$$N_2 = \frac{N_1 \lambda_2}{\lambda_1 \cdot 2} = \frac{2 \times 10^{15} \times 300}{600 \times 2}$$

$$n_2 = 5 \times 10^{14} \text{ per second}$$

14. **Statement (1)** : An electron in a uniform magnetic field, can move without changing its velocity vector.
Statement (2) : In the above case, the magnetic field should be along the direction of its velocity.
(1) Both statement 1 and statement 2 is correct, and statement 2 is the correct explanation of statement 1
(2) Both statement 1 and Statement 2 is correct but statement 2 is not the correct explanation of statement 1
(3) Statement 1 is correct, but statement 2 is incorrect
(4) Statement 1 is incorrect, but statement 2 is correct.

Ans. (1)

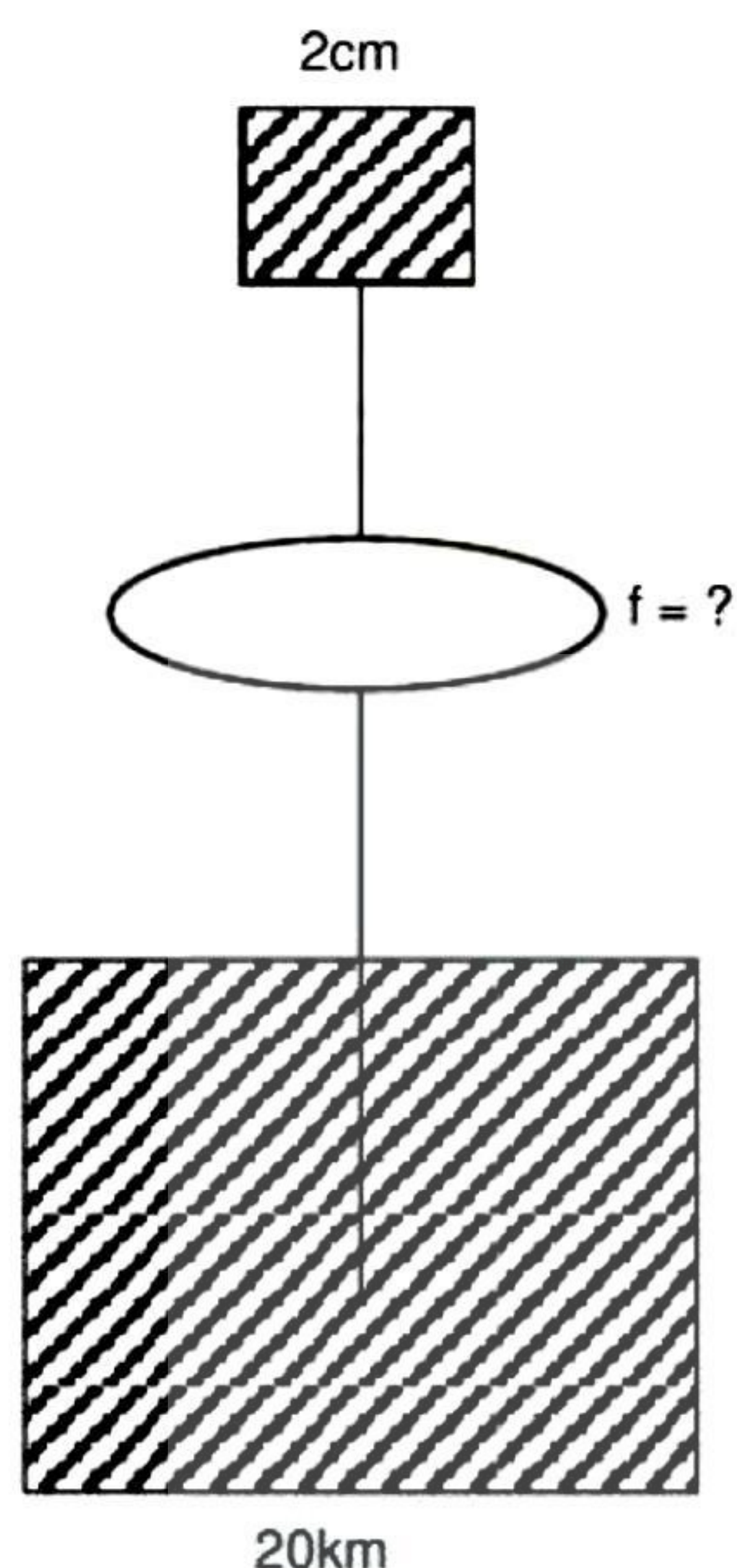
15. A drone camera situated at a height of 18 km, capture an image of area 400 km^2 , on a camera film of size $2 \text{ cm} \times 2 \text{ cm}$. find the focal length of the lens used in camera in mm.

- (1) 6 (2) 14 (3) 18 (4) 27

Ans. (3)

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Sol.



$$|m| = \frac{h_i}{h_o} = \frac{2\text{cm}}{20\text{km}} = \frac{2 \times 10^{-2}}{20 \times 10^3} = 10^{-6}$$

Since the image is real, so it will be inverted

$$m = -10^{-6} = \frac{-1}{10^6}$$

$$m = \frac{f}{f + u}$$

$$-\frac{10}{10^6} = \frac{f}{f + (-18\text{km})}$$

$$10^6 f = -f + 18 \text{ km}$$

$$10^6 f = 18 \text{ km}$$

$$f = \frac{18\text{km}}{10^6} = \frac{18 \times 10^3 \times 10^3 \text{mm}}{10^6}$$

$$f = 18 \text{ mm}$$

16. A spherical conductor carries a charge of $4 \times 10^{-8}\text{C}$ brought in contact with an uncharged spherical conductor and they are separated by a distance r . Now force between them is $9 \times 10^{-3} \text{ N}$. Determine the separation between the charges.

(1) 7

(2) 4

(3) 9

(4) 2

Ans. (4)

Sol.

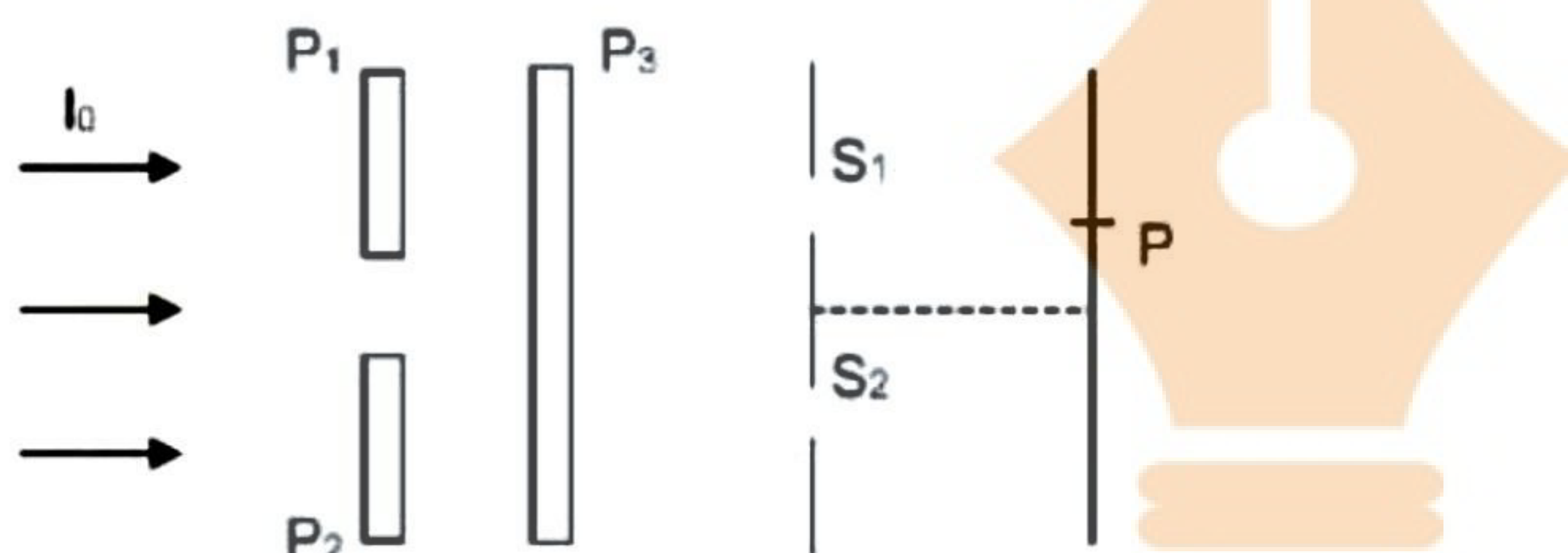


$$\frac{Kq^2}{R^2} = 9 \times 10^{-3}$$

$$\frac{9 \times 10^9 \times 2 \times 10^{-8} \times 2 \times 10^{-8}}{9 \times 10^{-3}} = R^2$$

$$R = 2 \text{ cm}$$

17.



In the following diagram polarizer P_1 & P_2 are orthogonal and P_3 is aligned at 45° w.r.t. P_1 and P_2 . If unpolarised light of intensity I_0 is incident on P_1 and P_2 and light after passing through P_3 is used in YDSE.

at some point P where path difference is $\frac{\lambda}{3}$, What is resultant intensity?

- (1) $\frac{I_0}{2}$ (2) $\frac{I_0}{3}$ (3) $\frac{I_0}{4}$ (4) I_0

Ans. (3)

Sol. Intensity after P_1 & P_2 is $\frac{I_0}{2}$ and after P_3 $\frac{I_0}{2} \cos^2 45 = \frac{I_0}{2} \left(\frac{1}{2} \right) = \frac{I_0}{4}$

$$\text{Now, } I_P = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \Delta\theta$$

$$= \frac{I_0}{4} + \frac{I_0}{4} + 2\frac{I_0}{4} \cos \left[\frac{2\pi}{\lambda} \left(\frac{\lambda}{3} \right) \right]$$

$$= \frac{I_0}{2} + \frac{I_0}{2} \left[-\frac{1}{2} \right]$$

$$I_P = \frac{I_0}{4}$$

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18. A hot body is placed in the surrounding of temperature 16°C . During first 4 minutes, its temperature falls from 40°C to 24°C , then find its temperature after 4 minutes.

- (1) 12°C (2) 22°C (3) 10°C (4) 18.7°C

Ans. (4)

Sol. $\left(\frac{dT}{dt}\right) = k(T - T_0)$

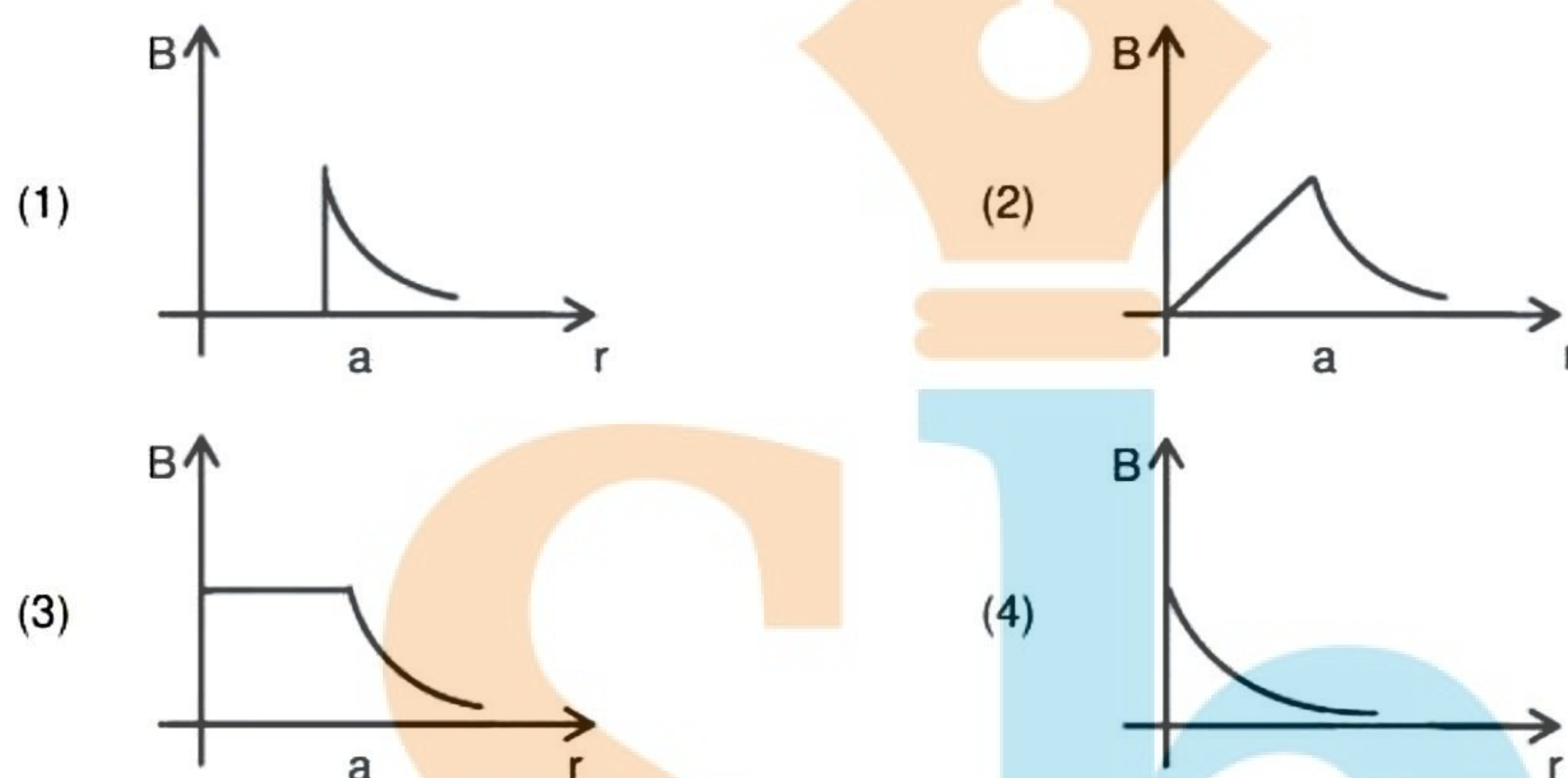
$$\left(\frac{40 - 24}{4 \text{ min}}\right) = k\left(\frac{24 + 40}{2} - 16\right) \quad \dots(i)$$

$$\left(\frac{24 - T}{4 \text{ min}}\right) = k\left(\frac{T + 24}{2} - 16\right) \quad \dots(ii)$$

Solving the equations we get

$$T = \frac{56}{3} = 18.7^\circ\text{C}$$

- 19.** An infinitely long wire has current 'i' and its radius is 'a'. Choose the correct graph for 'B' v/s 'r' where 'r' is distance from centre of wire



Ans. (2)

- 20.** The position vector of a particle varies with time as $\vec{r} = (5t^2\hat{i} - 5t\hat{j})$ m. The magnitude and direction of velocity at $t = 2$ will be ;

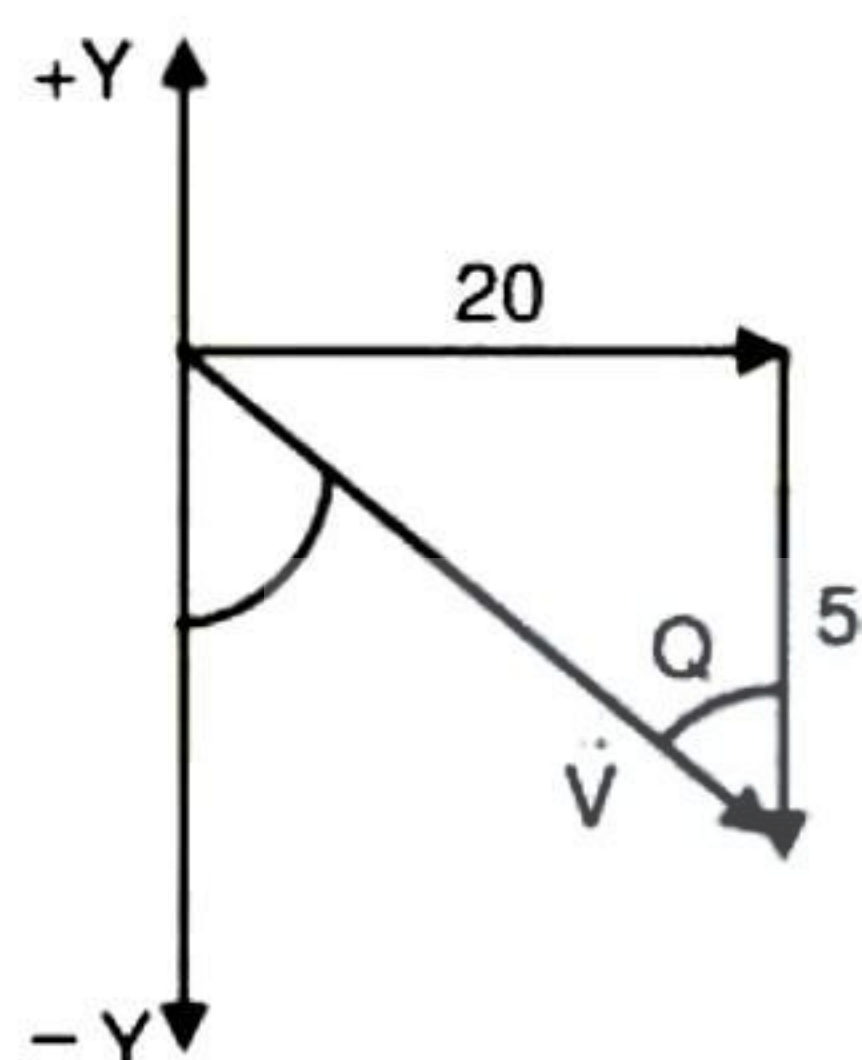
- (1) $5\sqrt{15}$
 (2) $5\sqrt{17}$ m/sec. at an angle of $\tan^{-1}(4)$ with $-y$ axis
 (3) $5\sqrt{17}$ m/sec. at an angle of $\tan^{-1}(4)$ with x axis
 (4) $5\sqrt{17}$ m/sec. at an angle of $\tan^{-1}(4)$ with $-x$ axis

Ans. (2)

Sol. $\vec{v} = \frac{d\vec{r}}{dt} = 10t\hat{i} - 5\hat{j}$

$$\vec{v}_{t=2} = 20\hat{i} - 5\hat{j} \Rightarrow |\vec{v}| = \sqrt{(20)^2 + (5)^2} = \sqrt{425}$$

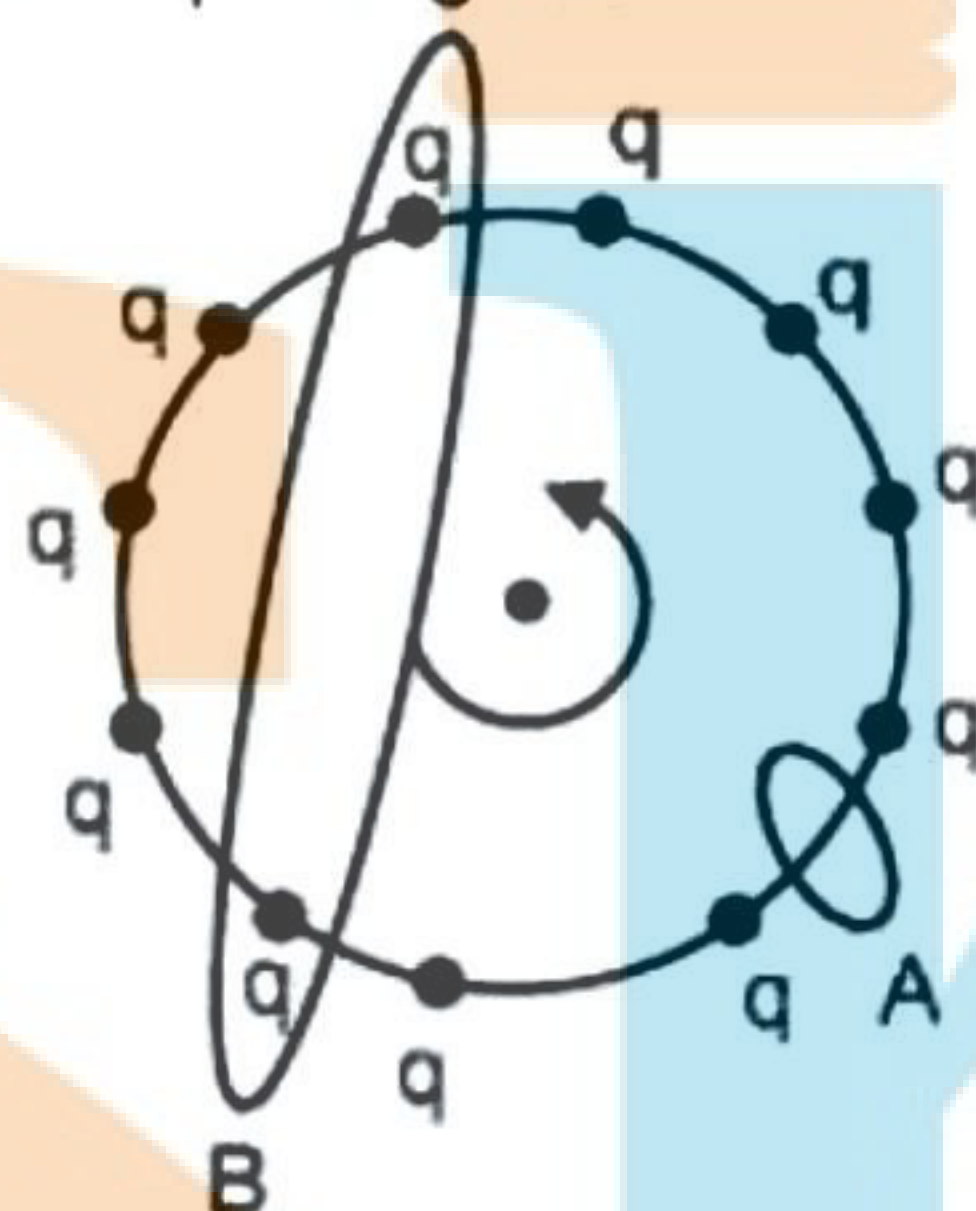
$$= 5\sqrt{17} \text{ m/sec}$$



$$\tan\theta = \frac{20}{5} = 4$$

$$\theta = \tan^{-1}(4) \text{ with } -y \text{ axis}$$

- 21.** Find the difference of the current ($I_A - I_B$). If n charge particles move in a circular path with ω angular velocity and there are two ampere's loop are given



where I_A is net current passing through the amperian loop A and I_B is the net current passing through loop B.

(1) $\frac{nq\omega}{2\pi}$

(2) $\frac{nq\omega}{\pi}$

(3) $\frac{2\pi\omega}{nq}$

(4) $\frac{2\pi}{nq\omega}$

Ans. (1)

Sol. In loop B incoming and outgoing current is equal & opposite so $I_B = 0$

$$T = \frac{2\pi}{\omega}$$

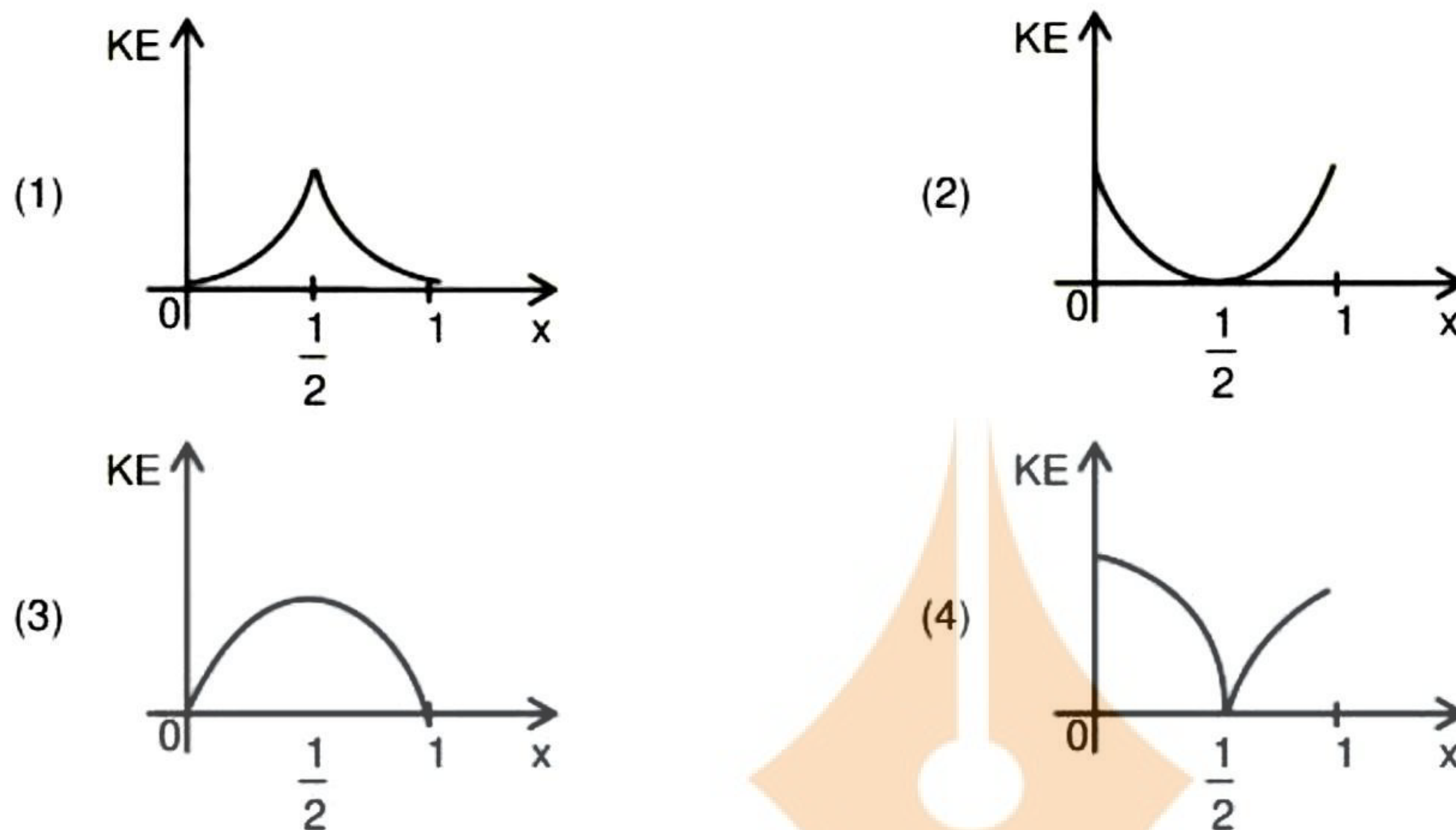
$$I_A = \frac{nq}{T}$$

$$I_A = \frac{nq\omega}{2\pi}$$

$$I_A - I_B = \frac{nq\omega}{2\pi}$$

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22. $x(t) = x_0 \sin^2\left(\frac{t}{2}\right)$ (where $x_0 = 1$) find graph of Kinetic energy v/s x



Ans. (3)

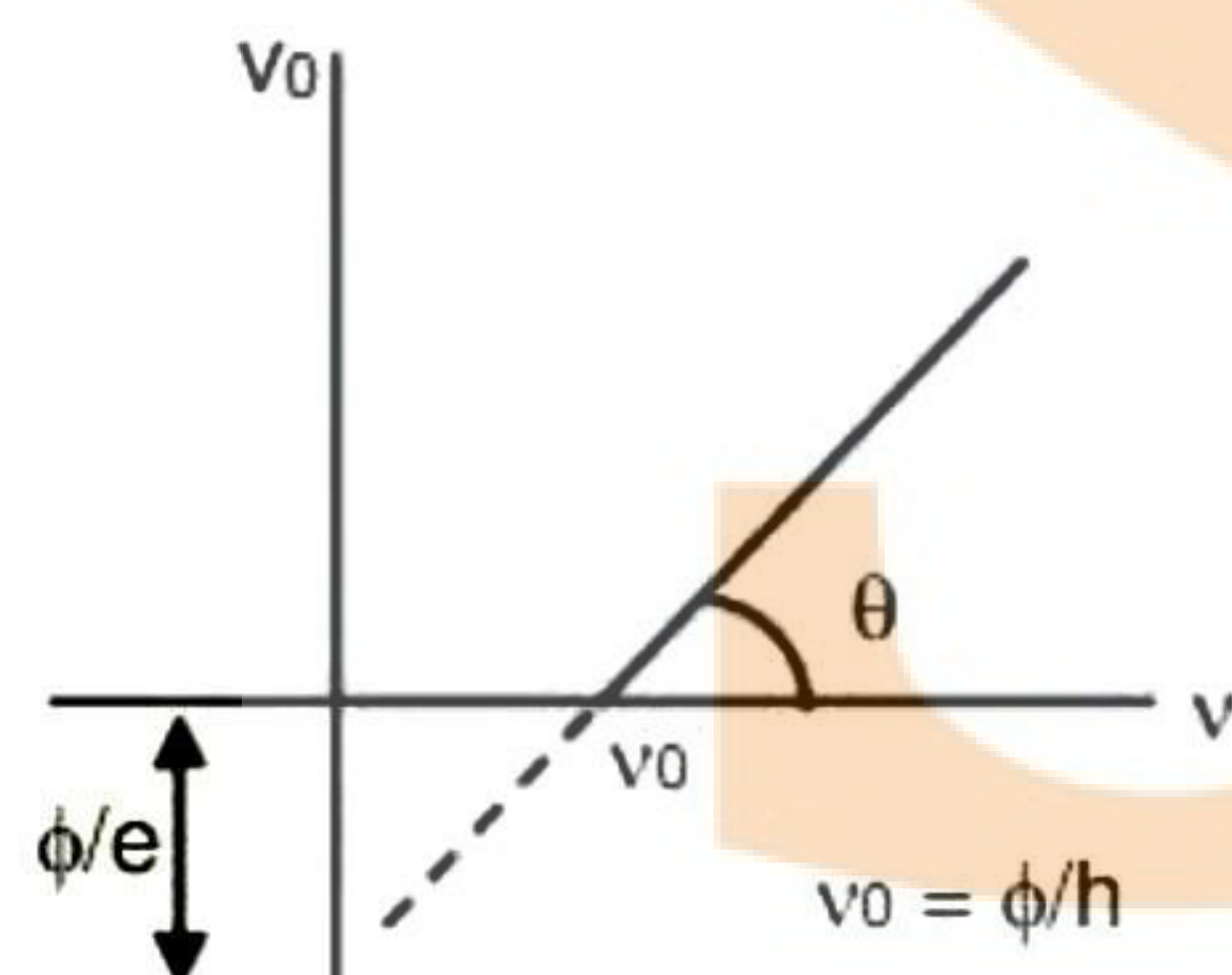
23. For the graph of stopping potential V_0 v/s frequency which statement is correct .
 (1) graph is linear
 (2) slope is d/h
 (3) h is related to slope
 (4) to find D , we don't require h .

Ans. (1)

Sol. $eV_0 = h\nu - h\nu_0$

$$V_0 = \frac{h\nu}{e} - \frac{h\nu_0}{e}$$

$$V_0 = \frac{h\nu}{e} - \frac{d}{e}$$



$$\tan\theta = \frac{h}{e} = \text{slope}$$

24. A electron is moving in a circular path inside a solenoid with a time period of 75 ns. The current through the solenoid is 1 amp. Determine the number of turns per unit length of solenoid.



(1) 3.8×10^3

(2) 38×10^3

(3) 4.3×10^3

(4) 43×10^3

Ans. (1)

Sol. We know that

$$B = \frac{2\pi m}{qT} = \frac{2 \times 3.14 \times 9.1 \times 10^{-31}}{1.6 \times 10^{-16} \times 75 \times 10^{-9}}$$

$$B = 4.78 \times 10^{-3} \text{ T}$$

$$\text{So, } n = \frac{B}{\mu_0 I} = \frac{B}{\mu_0 I} \frac{4.78 \times 10^{-3}}{4\pi \times 10^{-2} \times 1}$$

$$n = 3.8 \times 10^3$$

25. A material has a bulk modulus of $25 \times 10^{11} \text{ N/m}^2$. If it undergoes a volumetric strain of 0.2%, what is the excess pressure applied ?

(1) $5 \times 10^8 \text{ N/m}^2$

(2) $5 \times 10^9 \text{ N/m}^2$

(3) $5 \times 10^{10} \text{ N/m}^2$

(4) $5 \times 10^{11} \text{ N/m}^2$

Ans. (2)

Sol. The bulk modulus K of a material is defined by the formula :

$$K = \frac{\text{Excess Pressure}(P)}{\text{Volumetric Strain}(\Delta V/V)}$$

Given data :

Bulk modulus, $K = 25 \times 10^{11} \text{ N/m}^2$

Volumetric strain, $\frac{\Delta V}{V} = 0.002$

Rearranging the formula to solve for excess pressure :

$$P = K \times \left(\frac{\Delta V}{V} \right)$$

Thus, the excess pressure is :

$$5 \times 10^9 \text{ N/m}^2$$

Student Bro

PART : CHEMISTRY

1. Arrange the following in ascending order wavelength

λ_1 = Infrared

λ_2 = Micro

λ_3 = X-ray

λ_4 = U.V.

(1) $\lambda_3 < \lambda_4 < \lambda_1 < \lambda_2$ (2) $\lambda_3 < \lambda_1 < \lambda_4 < \lambda_2$ (3) $\lambda_2 < \lambda_1 < \lambda_4 < \lambda_3$ (4) $\lambda_1 < \lambda_4 < \lambda_2 < \lambda_3$

Ans. (1)

Sol. Order of wavelength in EM spectrum:

Cosmic < Gamma < X-rays < UV < Visible < Intra Red < Micro < Radio

2. $t_{2g}^3 e_g^1$ configuration is possible in:

(1) WFL; high spin

(2) WFL; low spin

(3) SFL; high spin

(4) SFL; low spin

Ans. (1)

Sol. WFL will not cause pairing & above is high spin arrangement (greater no. unpaired e^-).

3. When ethane -1, 2-diammine is progressive added to aqueous of Nickel (II) chloride the sequence of colour changed observed will be

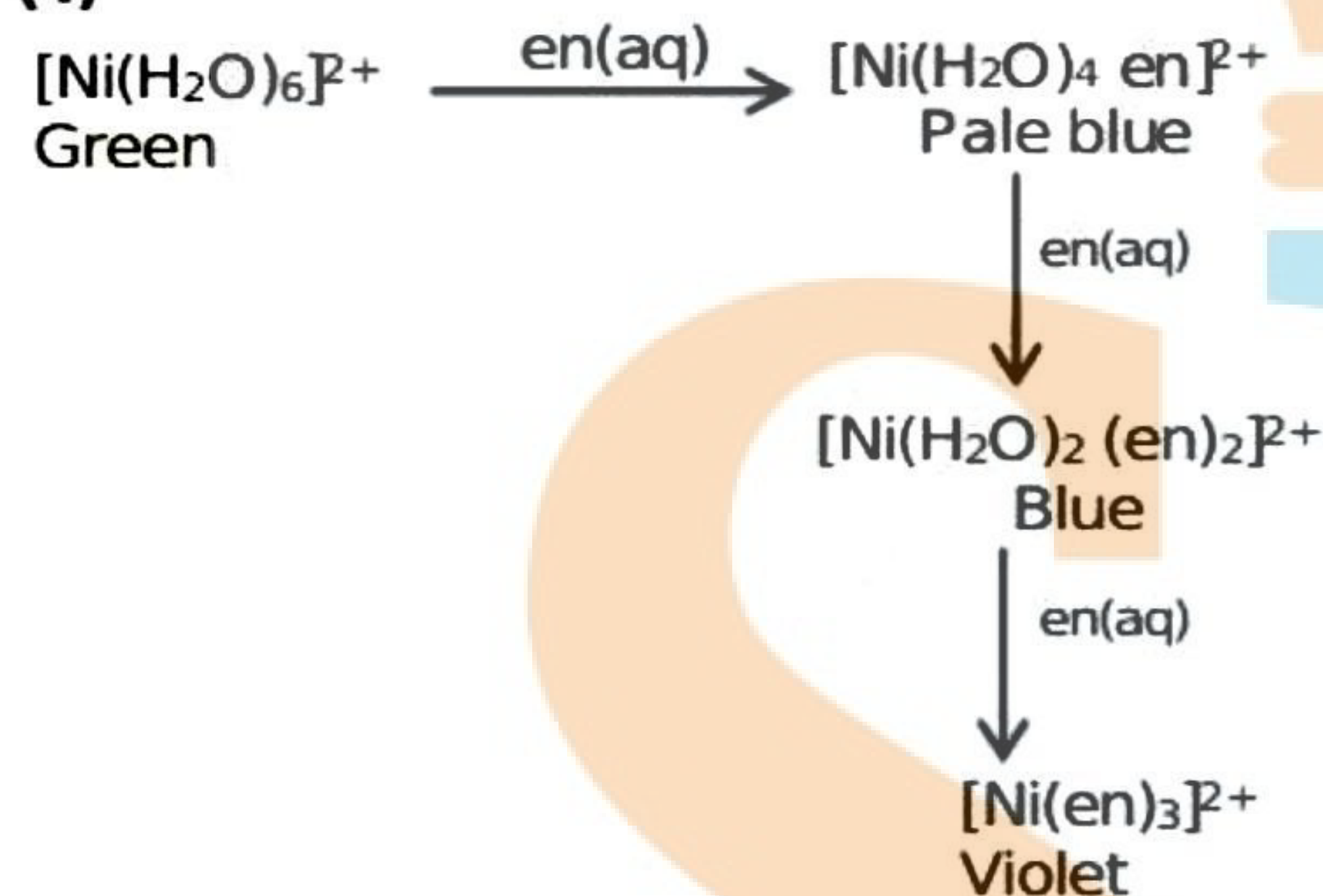
(1) Pale blue \rightarrow Blue \rightarrow Green \rightarrow Violet

(2) Violet \rightarrow Blue \rightarrow Pale blue \rightarrow Green

(3) Pale blue \rightarrow Blue \rightarrow Violet \rightarrow Green

(4) Green \rightarrow Pale blue \rightarrow Blue \rightarrow violet

Ans. (4)



Sol.

4. **Statement-I** : IE_1 of Sn > Pb

Statement-II : IE_1 of Si > Ge

(1) Both Statement I and statement II are true

(2) Both statement I and statement II are false

(3) Statement I is true but statement II is false

(4) Statement I is false but statement II is true

Ans. (4)

Sol. IE decreases down the gap. So Si > Ge & Pb, Sn exceptional

5. Compound $\xrightarrow{\text{aquaregia}} \text{B} \xrightarrow[\text{CH}_3\text{COOH}]{\text{KNO}_2} \text{Yellow ppt}$

(1) NiS

(2) ZnS

(3) CoS

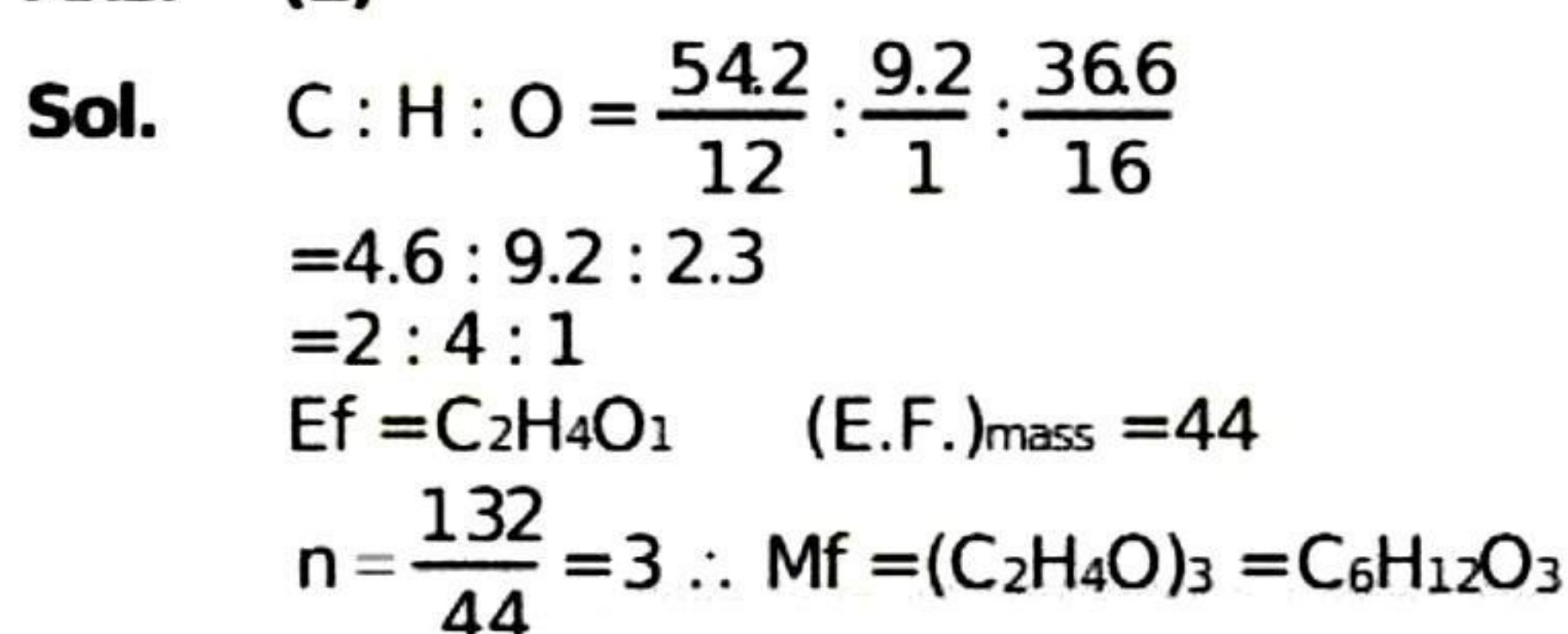
(4) MnS

Ans. (3)

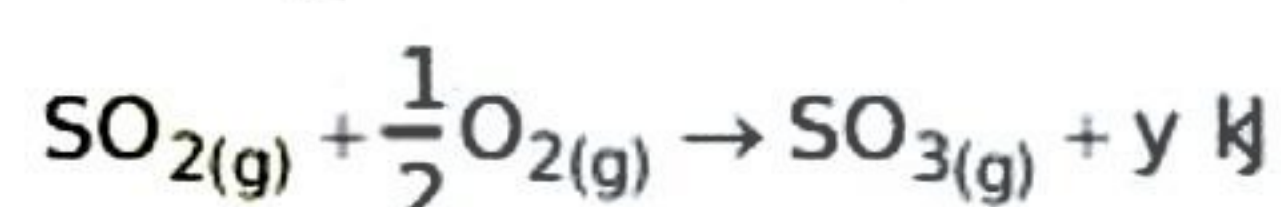
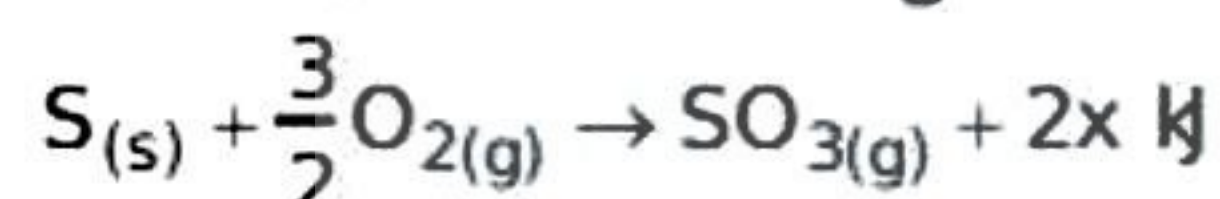
Sol. $\text{CoS} \xrightarrow{\text{aquaregia}} \text{CoCl}_2 \xrightarrow[\text{CH}_3\text{COOH}]{\text{KNO}_2} \text{K}_3[\text{Co}(\text{NO}_2)_6] \downarrow \text{Yellow}$

6. 54.2% C, 9.2% H & 36.6% O are present in a compound. If its molar mass is 132 g, its molecular formula is
 (1) $C_6H_{12}O_3$ (2) $C_4H_8O_2$ (3) $C_6H_{12}O_6$ (4) None of these

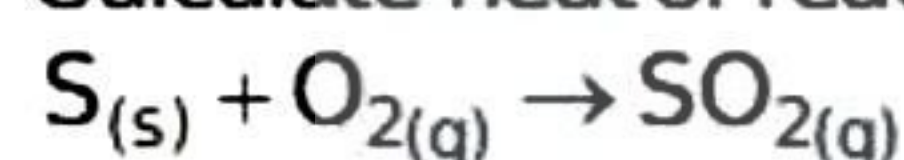
Ans. (1)



7. Consider the following reactions

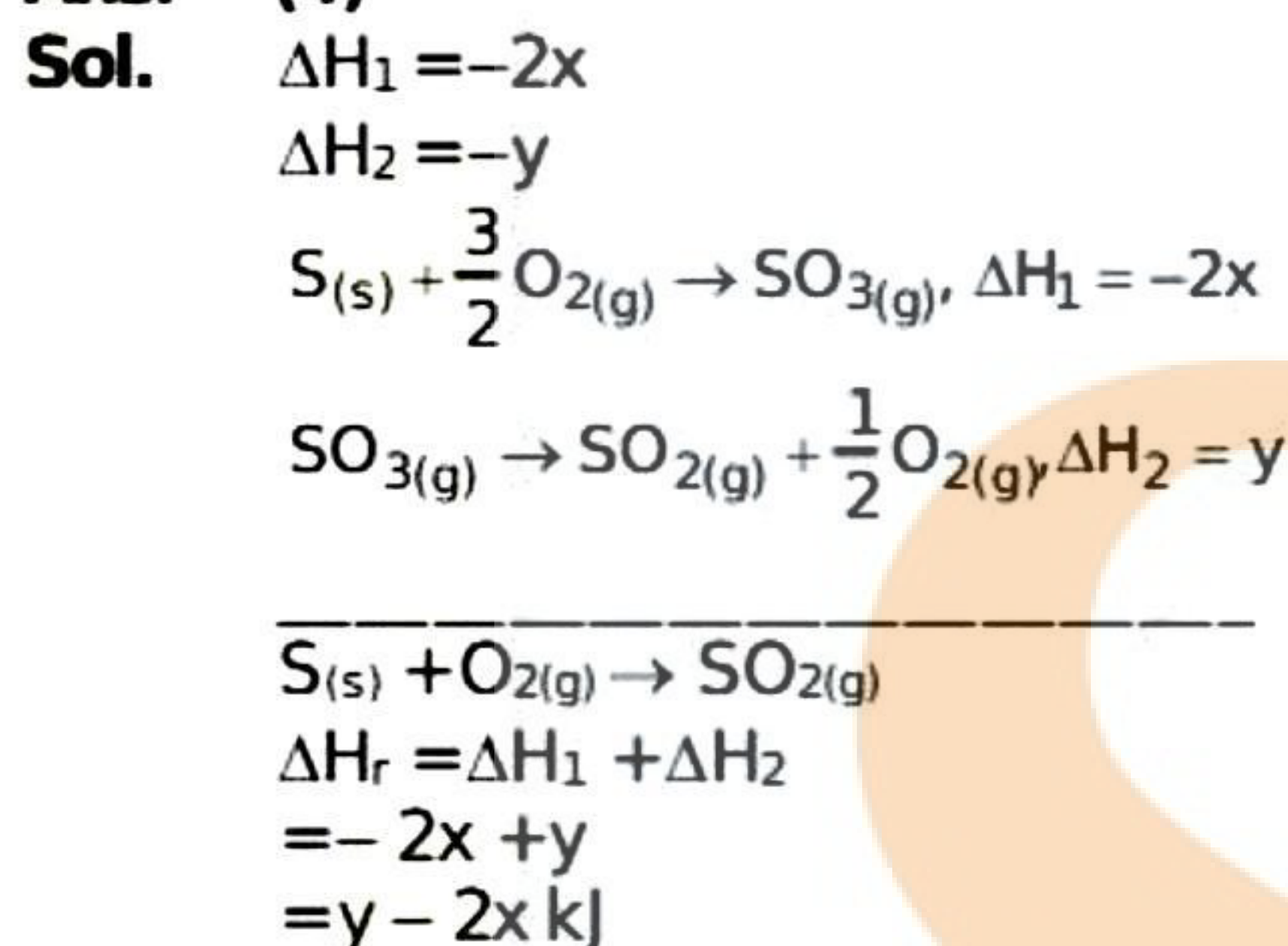


Calculate heat of reaction (kJ) for the given reaction



- (1) $-(x + y)$ (2) $-(2x + y)$ (3) x/y (4) $y - 2x$

Ans. (4)



8. Match the following cations with respective spin magnetic moment

Ions	H(B.M)
(i) Ti^{3+}	(p) 2.83
(ii) Sc^{+3}	(q) 0.00
(iii) V^{+2}	(r) 1.73
(iv) Ni^{+2}	(s) 3.87

- (1) i-r; ii-q; iii-s; iv-p
 (2) i-p; ii-q; iii-r; iv-s
 (3) i-s; ii-p; iii-q; iv-r
 (4) i-s; ii-p; iii-r; iv-q

Ans. (1)

9. Calculate the overall activation energy

$$K = \frac{k_1 k_3}{k_2}$$

$E_{a_1} = 60 \text{ kJ}$
 $E_{a_2} = 40 \text{ kJ}$
 $E_{a_3} = 20 \text{ kJ}$

Ans. (20)

Sol.
$$e^{-E_a/RT} = \sqrt{\frac{e^{-E_{a1}/RT} \cdot e^{-E_{a3}/RT}}{e^{-E_{a2}/RT}}}$$

$$e^{-E_a/RT} = \sqrt{e^{\frac{(E_{a2} - E_{a1} - E_{a3})}{RT}}}$$

$$-E_a = (E_{a2} - E_{a1} - E_{a3}) \times \frac{1}{2}$$

$$E_a = (E_{a1} + E_{a3} - E_{a2}) \times \frac{1}{2}$$

$$E_a = \frac{1}{2}(60 + 20 - 40) = 20 \text{ kJ}$$

10. Statement-I : Oxygen-oxygen bond length in O_3 is greater than O_2 .

Statement-II : O-O bond order in O_3 is 1.5 and O-O bond order in O_2 is 2.

- (1) Both Statement I and statement II are true (2) Both statement I and statement II are false
 (3) Statement I is true but statement II is false (4) Statement I is false but statement II is true

Ans. (1)

11. The successive ionisation energy (I.E.) of an element 'X' is given

	IE ₁	IE ₂	IE ₃	IE ₄	IE ₅
X →	500	600	2000	2200	2600

Data given in kJ/mol.

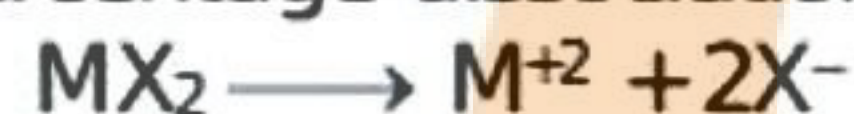
Find out the group number of element X.

- (1) Group-13 (2) Group-14 (3) Group-2 (4) Group-13

Ans. (3)

12. MX_2 observed molar mass: 65.6 Normal molar mass: 164

Find percentage dissociation.



Ans. (78)

Sol.
$$i = \frac{\text{normal molar mass}}{\text{abnormal molar mass}} = \frac{164}{65.6} = 2.5$$

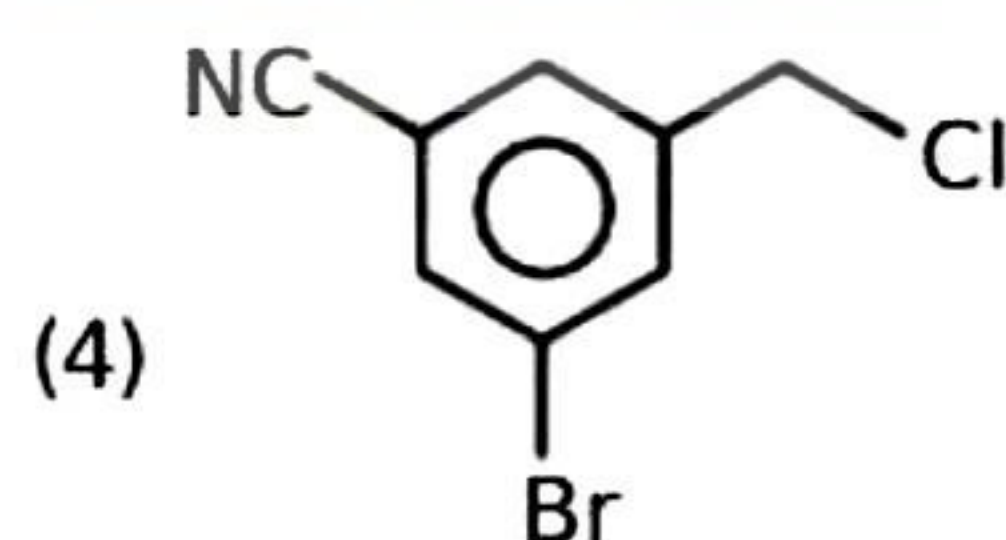
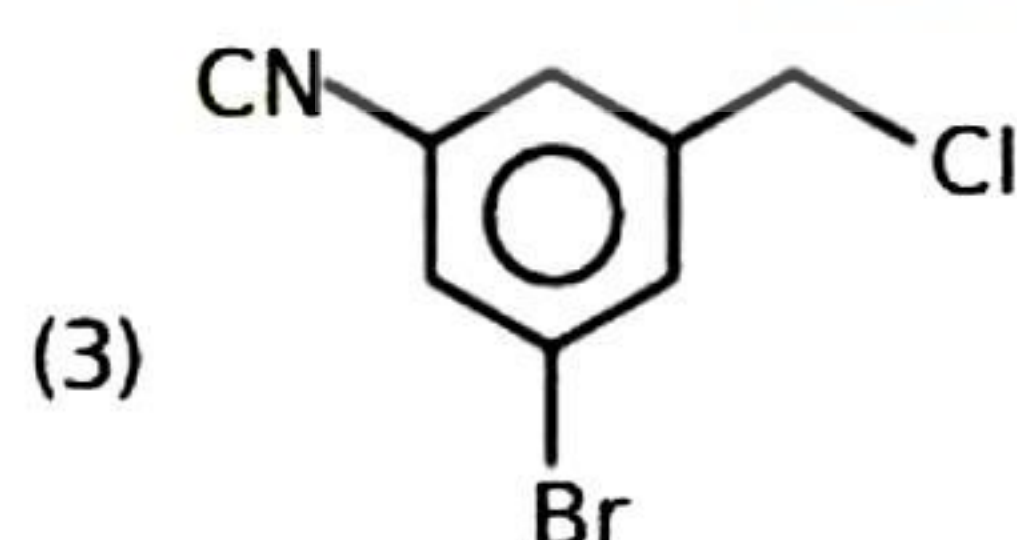
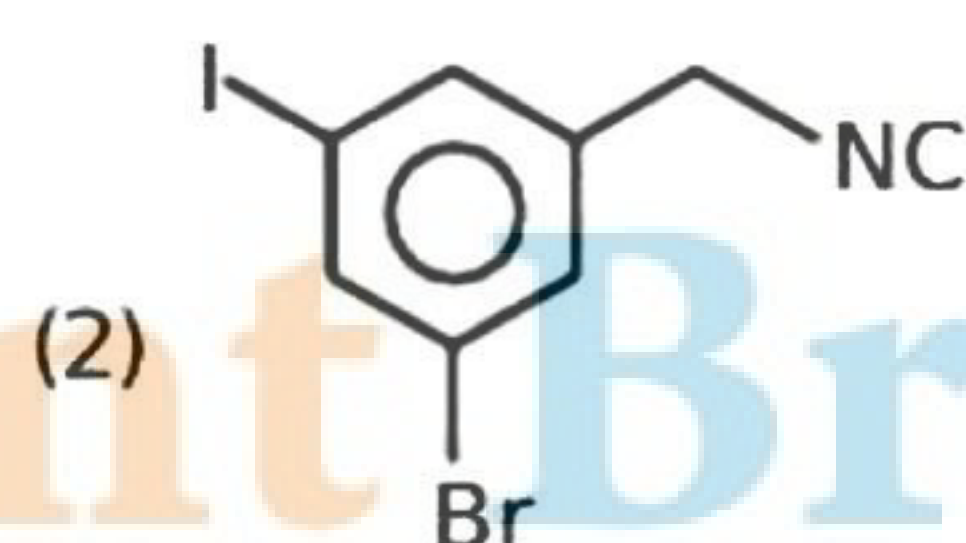
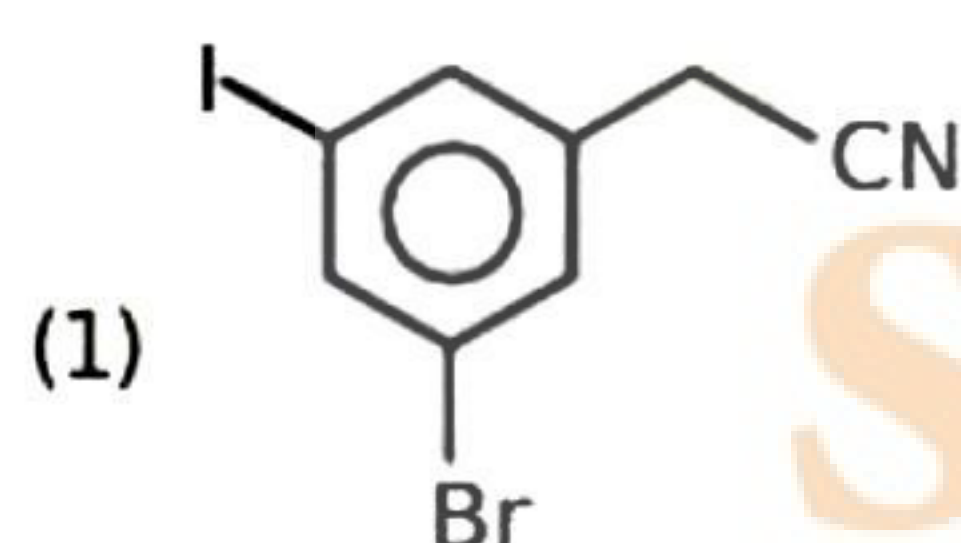
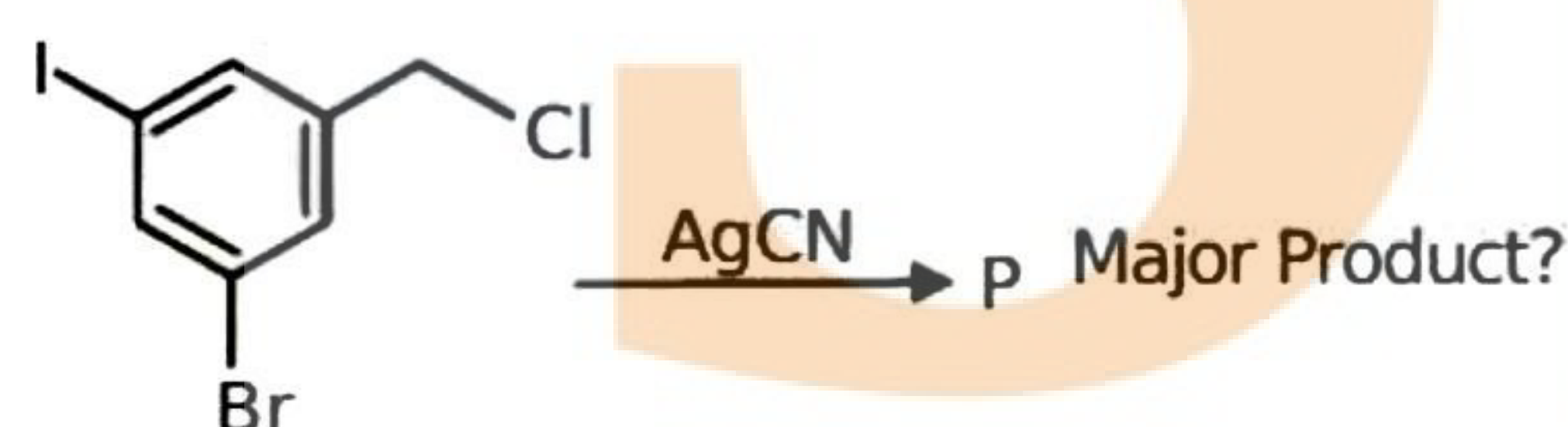
$$2.5 = 1 + 2\alpha$$

$$1.5 = 2\alpha$$

$$\alpha = 0.75$$

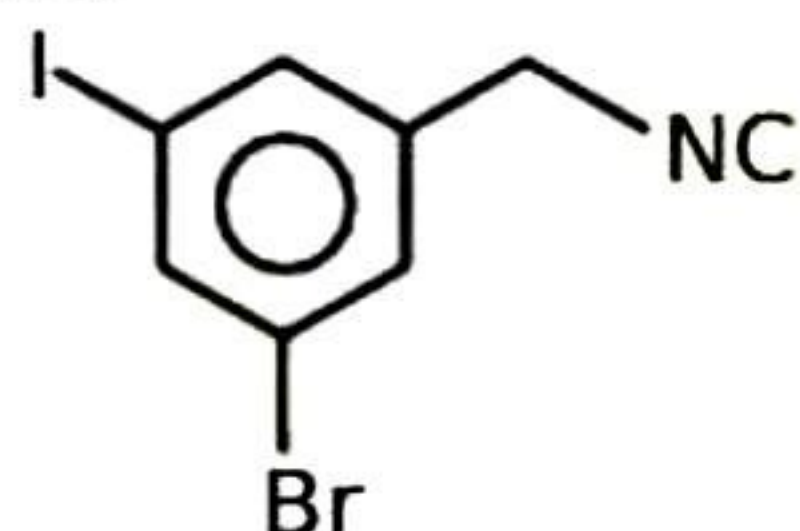
$$\% \alpha = 75$$

13.



Ans. (2)

Sol.



14. Match the following reactions given in Column-I with respective reagents given in Column-II.

Column-I

- (a) Etard Reaction
- (b) Gattermann Reaction
- (c) Gattermann Koch Reaction
- (d) Staphen Reaction

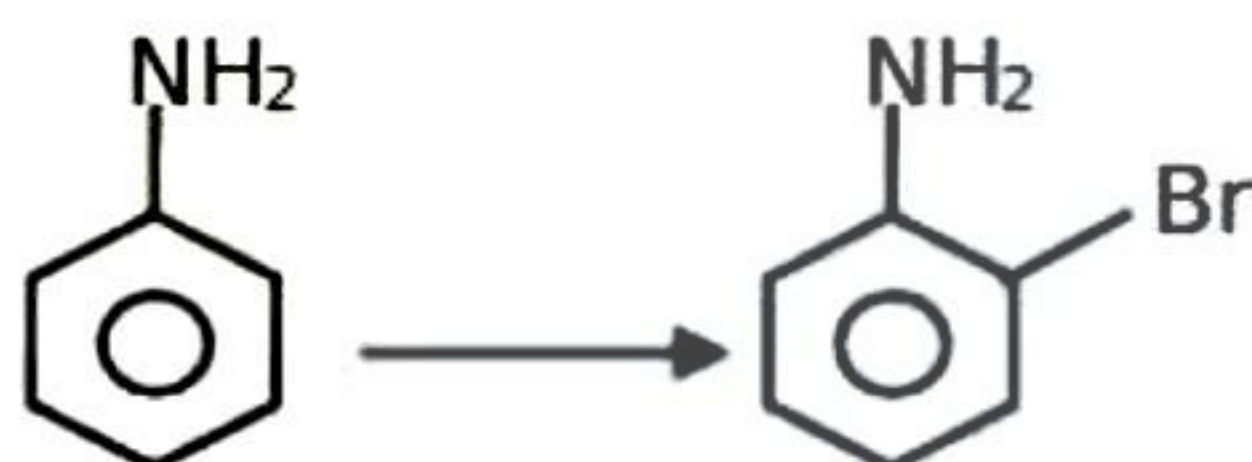
Column-II

- (p) $\text{SnCl}_2 + \text{HCl}$
- (q) CrO_2Cl_2
- (r) $\text{Cu} + \text{HCl}$
- (s) $\text{CO} + \text{HCl}$, Anhydrous AlCl_3

- (1) a-(q); (b)-(r); (c)-(s); (d)-(p)
- (2) a-(p); (b)-(q); (c)-(r); (d)-(s)
- (3) a-(q); (b)-(s); (c)-(p); (d)-(r)
- (4) a-(p); (b)-(r); (c)-(q); (d)-(s)

Ans. (1)

15.

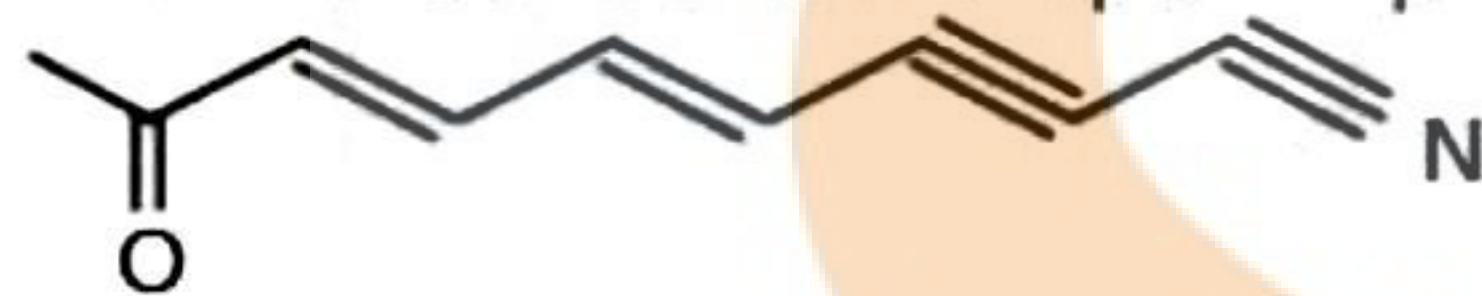


Above conversion can be done by using which reagents among the following.

- (1) Fe/Br_2 , $\text{H}_2\text{O}(\Delta)$, H_2SO_4
- (2) Ac_2O , H_2SO_4 , Br_2 , NaOH
- (3) Ac_2O , Br_2/AcOH , $\text{H}_2\text{O}/\text{H}^+$
- (4) Ac_2O , Br_2/Fe , NaOH

Ans. (2)

16. Find the total number of sp and sp^2 hybridised carbon atoms in the given compound.



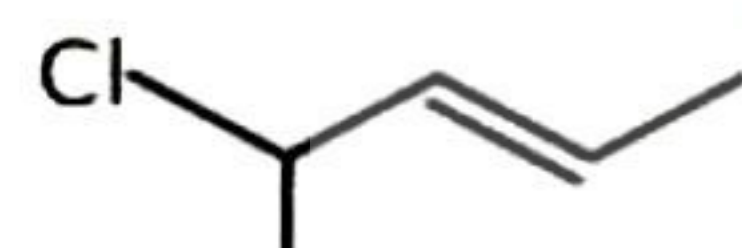
Ans. (8)

Sol. $\text{sp}^2 = 5$
 $\text{sp} = 3$
Total = 8

17. In the carius method, 0.25 gm organic compound is heated with fuming HNO_3 then AgNO_3 is added it gives 0.15 gm AgBr if molecular mass of AgBr is 188 then find mass percentage of Br in that organic compound

Ans. (25.53%)

18.



Find total number of stereoisomers of the given compound.

Ans. (4)

19. Match the following Nitrogenous Bases with their respective structures.

Column-I

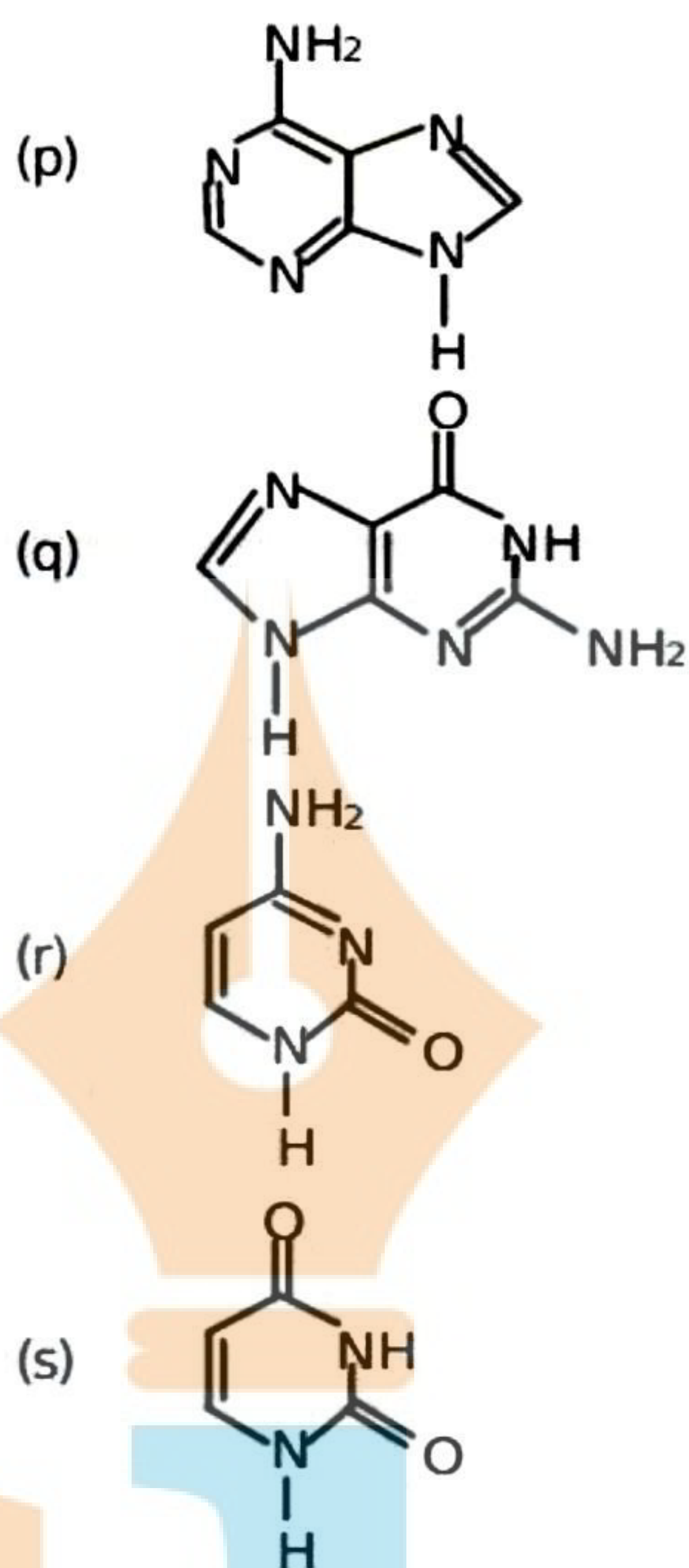
(a) Cytosine

(b) Uracil

(c) Guanine

(d) Adenine

Column-II



(1) a-(q); (b)-(r); (c)-(s); (d)-(p)

(2) a-(r); (b)-(s); (c)-(q); (d)-(p)

(3) a-(q); (b)-(s); (c)-(p); (d)-(r)

(4) a-(p); (b)-(r); (c)-(q); (d)-(s)

Ans.

(2)

20.

A hydrocarbon X that has molar mass 80 gm contains 90% carbon. Find degree of unsaturation in X.

Ans.

(3)

Student Bro

PART : MATHEMATICS

1. If $7 = 5 + \frac{1}{7} (5 + a) + \frac{1}{7^2} (5 + 2a) + \dots \infty$ term then the value of a is:

Ans. (6)

Sol. $7 = 5 + \frac{1}{7} (5 + a) + \frac{1}{7^2} (5 + 2a) + \dots \infty$ (i)

multiply with $\frac{1}{7}$ ever term.

$$\frac{7}{7} = \frac{5}{7} + \frac{1}{7^2} (5 + a) + \dots \infty \quad \text{..... (ii)}$$

subtract from equation (i)equation (ii)

$$7 - \frac{7}{7} = 5 + \frac{1}{7} (a) + \frac{1}{7^2} (a) + \dots \infty$$

$$6 = 5 + \frac{1}{7} a [1 + \frac{1}{7} + \dots \infty]$$

$$1 = \frac{1}{7} a \left[\frac{1}{1 - \frac{1}{7}} \right]$$

$$1 = \frac{1}{7} a \times \frac{7}{6}$$

$$a = 6$$

2. If A and B are binomial coefficients of 30th and 12th term of binomial expansion $(1 + x)^{2n-1}$. If $2A = 5B$, then the value of n is:

(1) 19

(2) 20

(3) 21

(4) 40

Ans. (3)

Sol.

$$T_{30} = {}^{2n-1}C_{29} \cdot x^{29}, \quad A = {}^{2n-1}C_{29}$$

$$T_{12} = {}^{2n-1}C_{11} \cdot x^{11}, \quad B = {}^{2n-1}C_{11}$$

$$2A = 5B$$

$$\Rightarrow 2 \times {}^{2n-1}C_{29} = 5 \cdot {}^{2n-1}C_{11}$$

$$\Rightarrow \frac{2}{(2n-30)! \cdot 29!} = \frac{5}{(2n-12)! \cdot 11!}$$

$$n = 21.$$

3. In a arithmetic progression S_n represent the sum of n terms and $S_{12} = 57$, $S_{40} = 1030$ then the value of $S_{30} - S_{10}$ is:

Ans. (515)

Sol.

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$S_{12} = \frac{12}{2} [2a + 11d] = 57$$

$$2a + 11d = \frac{19}{2} \quad \dots(1)$$

$$S_{40} = \frac{40}{2} [2a + 39d] = 1030$$

$$2a + 39d = \frac{103}{2} \quad \dots(2)$$

Equation (2) – (1)

$$39d - 11d = \frac{103}{2} - \frac{19}{2}$$

$$d = \frac{3}{2}, a = \frac{-7}{2} \text{ now}$$

$$S_{30} - S_{10} = 15 [2a + 29d] - 5 [2a + 9d] = 20a + 390d$$

$$= 20 \times \left(\frac{-7}{2}\right) + 390 \times \left(\frac{3}{2}\right) = 515$$

4. Equation of the chord having mid point (3, 1) to the ellipse $\frac{x^2}{25} + \frac{y^2}{16} = 1$ is :

$$(1) 25x + 5y - 125 = 0$$

$$(2) 48x + 25y - 169 = 0$$

$$(3) 65x + 2y - 12 = 0$$

$$(4) 45x + 4y - 135 = 0$$

Ans. (2)

Sol. $S_1 = T$

$$= \frac{3^2}{25} + \frac{1^2}{16} - 1 = \frac{3x}{25} + \frac{y}{16} - 1$$

$$= \frac{9}{25} + \frac{1}{16} = \frac{3x}{25} + \frac{y}{16}$$

$$= 48x + 25y - 169 = 0$$

5. Let $A = [a_{ij}]_{2 \times 2}$ such that $a_{ij} \in \{0, 1\}$. Probability that randomly chosen such matrix A is non-invertible is

$$(1) \frac{3}{8}$$

$$(2) \frac{5}{8}$$

$$(3) \frac{1}{2}$$

$$(4) \frac{7}{8}$$

Ans. (2)

Sol. Total number of matrices $A = 2^4 = 16$

$$\text{Let } A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$$

For non-invertible matrix $|A| = 0 \Rightarrow$

$$ad - bc = 0$$

$$ad = bc$$

Case 1

\Rightarrow

$$ad = bc = 0$$

$$({}^2C_1 + {}^2C_2) ({}^2C_1 + {}^2C_2) = 9$$

Case 2

\Rightarrow

$$ad = bc = 1$$

$$1 \times 1 = 1$$

$$\text{Required probability} = \frac{9+1}{16} = \frac{5}{8}$$

6. If system of equations

$$x + 2y - 3z = 2$$

$$2x + \lambda y + 5z = 5$$

$$4x + 3y + \mu z = 33$$

has infinite many solutions then $\lambda + \mu$ is

(1) $\frac{244}{5}$

(2) $\frac{1334}{5}$

(3) $\frac{1296}{5}$

(4) $\frac{4997}{5}$

Ans. (2)

Sol. $\Delta = 0 \quad \Delta = \begin{vmatrix} 1 & 2 & -3 \\ 2 & \lambda & 5 \\ 4 & 3 & \mu \end{vmatrix} = 0$

$$12\lambda + \lambda\mu - 4\mu + 7 = \dots\dots\dots(i)$$

$$\Delta z = \begin{vmatrix} 1 & 2 & 2 \\ 2 & \lambda & 5 \\ 4 & 3 & 33 \end{vmatrix} = 0$$

$$\lambda = \frac{19}{5}$$

from (i) $\mu = 263$

$$\lambda + \mu = \frac{19}{5} + 263 = \frac{1334}{5}$$

7. The area bounded by $y = e^x$, $y = |e^x - 1|$ and y-axis is ____

(1) $\ln 2$

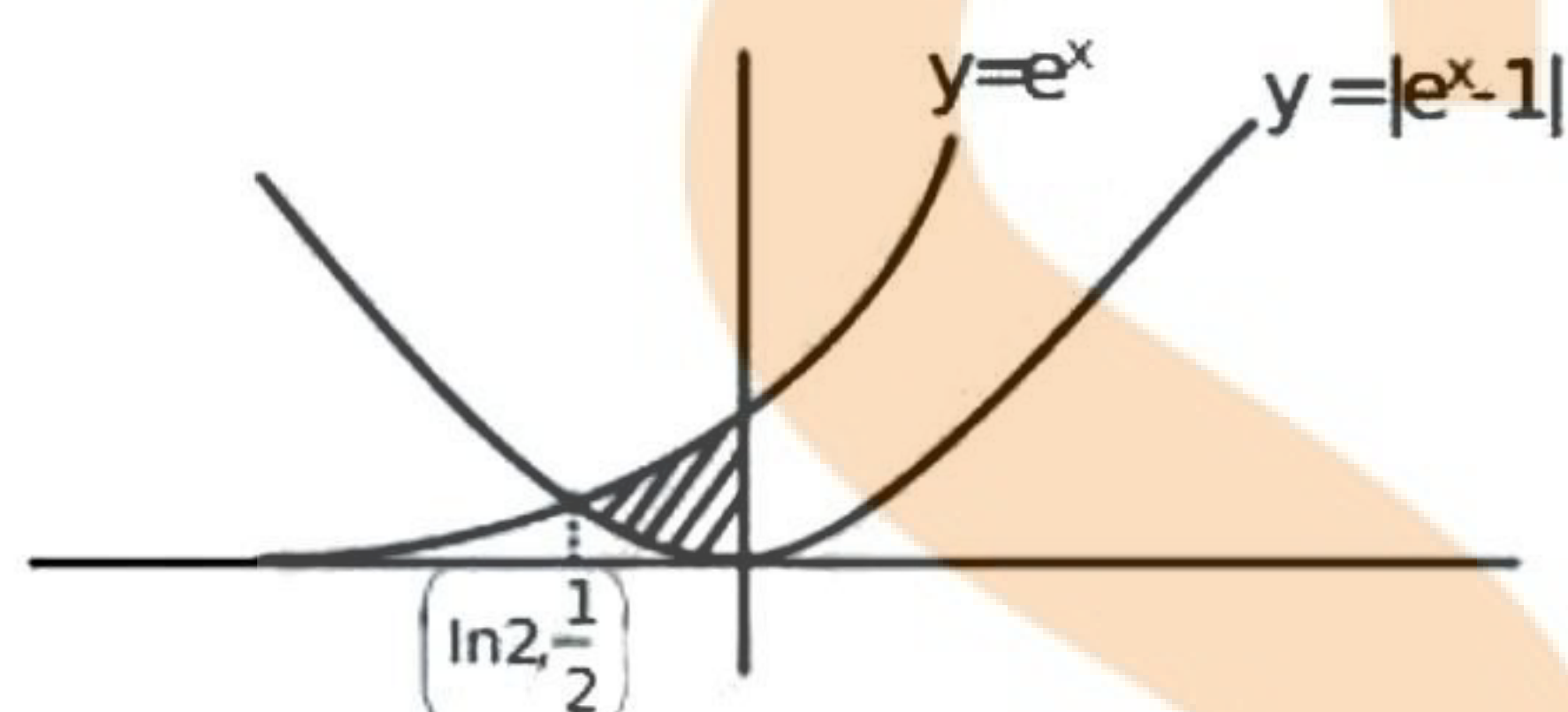
(2) $1 + \ln 2$

(3) $1 - \ln 2$

(4) $2\ln 2$

Ans. (3)

Sol.



$$e^x = 1 - e^x$$

$$e^x = \frac{1}{2}$$

$$x = -\ln 2$$

$$\text{required area} = \int_{-\ln 2}^0 (e^x - (1 - e^x)) dx = [2e^x - x]_{-\ln 2}^0$$

$$= 2 - (2e^{-\ln 2} + \ln 2) = 2 - 1 - \ln 2 = 1 - \ln 2$$

8. $f(x) = [x] + |x - 2|$; $-2 < x < 3$
and m = number of points of discontinuity, and
 n = number of points of non differentiability.

Then the value of $m + n$ is:

(1) 8

(2) 7

(3) 9

(4) - 10

Ans. (1)

Sol. $f(x) = \begin{cases} -x & ; x \in (-2, -1) \\ 1-x & ; x \in [-1, 0) \\ 2-x & ; x \in [0, 1) \\ 3-x & ; x \in [1, 2) \\ x & ; x \in [2, 3) \end{cases}$

As we can see that function is discontinuous at $-1, 0, 1$ and 2 .

Therefore, function is non-differentiable at $-1, 0, 1$ and 2 .

Therefore, $m = 4$ and $n = 4$.

Then, $m + n = 8$.

- 9.** There is a group A of 5 boys and 3 girls and another group B of 5 boys and 6 girls. How many ways can we invite 4 boys and 4 girls for party with 5 from group A and 3 from group B.

(1) 2850

(2) 2550

(3) 3150

(4) 3450

Ans. (3)

Sol. Group A \Rightarrow 5B, 3G

Group B \Rightarrow 5B, 6G

4 Boys and 4 girls invite

5 from group A and 3 from group B

Case (i)	In group A	4B 1G	In B	0B 3G
	In group A	3B 2G	In B	1B 2G
	In group A	2B 3G	In B	2B 1G
	In group A	1B 4G	In B	3B 0G (not possible)

We have three cases than.

$${}^5C_4 \times {}^3C_1 \times {}^5C_0 \times {}^6C_3 = 5 \times 3 \times 1 \times 20 = 300$$

$${}^5C_3 \times {}^3C_2 \times {}^5C_1 \times {}^6C_2 = 10 \times 3 \times 5 \times 15 = 2250$$

$${}^5C_2 \times {}^3C_3 \times {}^5C_2 \times {}^6C_1 = 10 \times 1 \times 10 \times 6 = 600$$

$$300 + 2250 + 600 = 3150$$

- 10.** $2\cos x \frac{dy}{dx} = \sin 2x - 2y \sin x$, $y(x) = y$ and $y(0) = 0$, then find the value of $y\left(\frac{\pi}{4}\right) + y\left(\frac{\pi}{4}\right)$ is:

(1) $\frac{1}{2}$

(2) $\frac{1}{\sqrt{2}}$

(3) $-\frac{1}{2}$

(4) $-\frac{1}{\sqrt{2}}$

Ans. (2)

Sol. $(2\cos x) y' (x) = \sin 2x - 2y(x) \sin x$

Put $x = \frac{\pi}{4}$

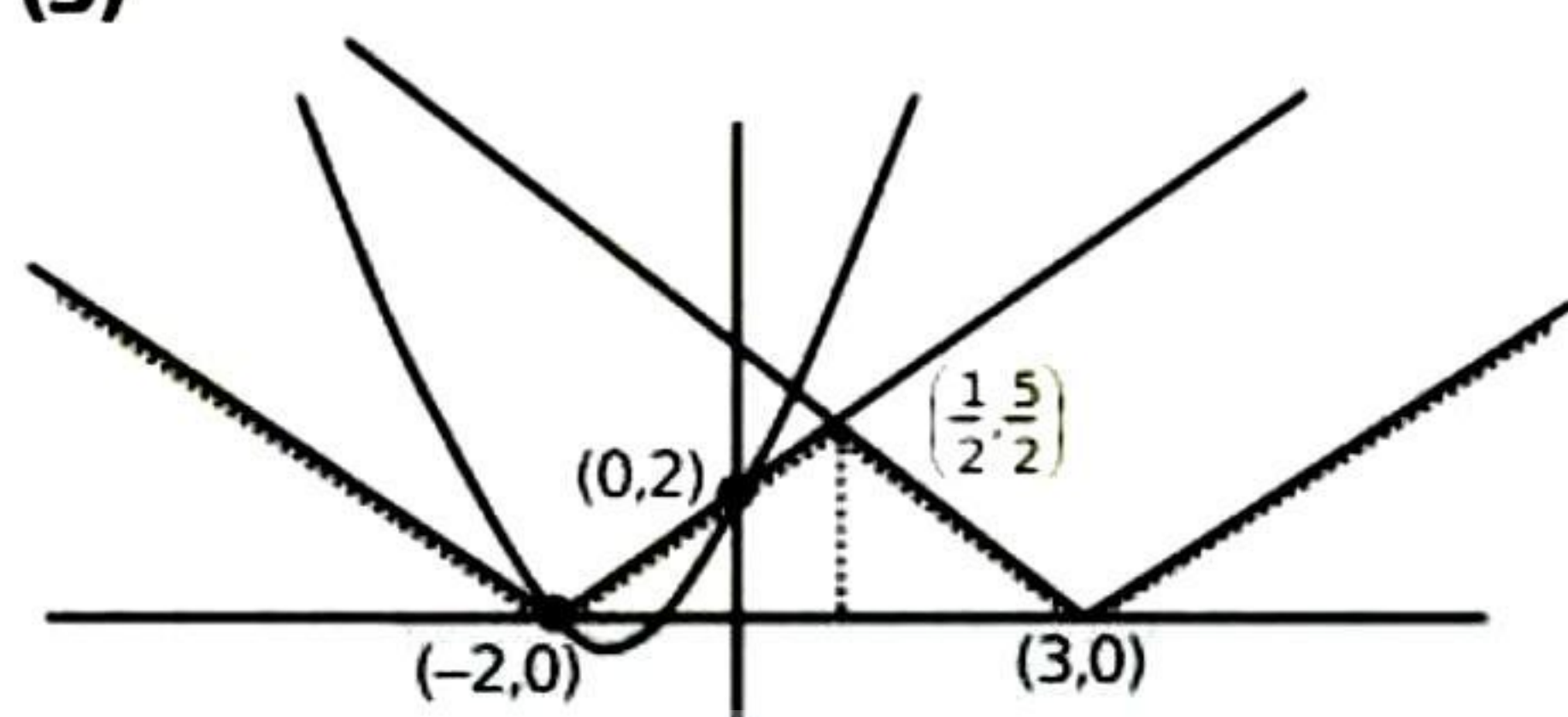
$$2 \times \frac{1}{\sqrt{2}} y\left(\frac{\pi}{4}\right) = 1 - 2y\left(\frac{\pi}{4}\right) \times \frac{1}{\sqrt{2}}$$

$$y\left(\frac{\pi}{4}\right) + y\left(\frac{\pi}{4}\right) = \frac{1}{\sqrt{2}}$$

11. Number of real solutions of the equation $x^2 + 3x + 2 = \min\{|x - 3|, |x + 2|\}$ is _____
 (1) 0 (2) 1 (3) 2 (4) 3

Ans. (3)

Sol.



Total number of solutions = 2

12. Consider the differential equation $x^2 \frac{dy}{dx} = 2xy + 3$ such that $y(1) = 4$ then the value of $2(y(2))$ is

Ans. (39)

Sol.

Divide by x^2

$$\frac{dy}{dx} - \frac{2}{x}y = \frac{3}{x^2}$$

$$\text{I.F.} = e^{\int \frac{-2}{x} dx} = e^{-2 \ln x} = e^{\ln x^{-2}} = \frac{1}{x^2}$$

$$y \cdot \text{I.F.} = \int \frac{3}{x^2} \cdot \text{I.F.} dx$$

$$\frac{y}{x^2} = 3 \int \frac{dx}{x^4}$$

$$\frac{y}{x^2} = \frac{-1}{x^3} + C$$

$$y(1) = 4 \Rightarrow 4 = -1 + C \Rightarrow C = 5$$

$$\frac{y}{x^2} = \frac{-1}{x^3} + 5$$

$$y = -\frac{1}{x} + 5x^2$$

$$y(2) = -\frac{1}{2} + 20 = \frac{39}{2}$$

$$2y(2) = 39$$

13. If

$$\lim_{x \rightarrow 0} \begin{vmatrix} a + \frac{\sin x}{x} & 1 & b \\ a & 1 + \frac{\sin x}{x} & b \\ a & 1 & b + \frac{\sin x}{x} \end{vmatrix} = \lambda a + \mu b + C$$

where λ and μ are the coefficient of a , b and c is constant then find the value of $(\lambda + \mu + c)^2$

Ans. (16)

Sol.

$$\Rightarrow \begin{vmatrix} a+1 & 1 & b \\ a & 1+1 & b \\ a & 1 & b+1 \end{vmatrix} = \lambda a + \mu b + C$$

$$R_1 \rightarrow R_1 - R_2$$

$$R_2 \rightarrow R_2 - R_3$$

$$\begin{vmatrix} 1 & -1 & 0 \\ 0 & 1 & -1 \\ a & 1 & b+1 \end{vmatrix} = \lambda a + \mu b + C$$

$$C_2 \rightarrow C_1 + C_2$$

$$\begin{vmatrix} 1 & 0 & 0 \\ 0 & 1 & -1 \\ a & a+1 & b+1 \end{vmatrix} = \lambda a + \mu b + C$$

$$a + b + 2 = \lambda a + \mu b + C$$

$$\text{So } \lambda = 1, \mu = 1, C = 2$$

$$\text{Now, } (\lambda + \mu + C)^2 = 16$$

14. If $f: (-\infty, \infty) \rightarrow (-\infty, 1)$, and $f(x) = \frac{2^x - 2^{-x}}{2^x + 2^{-x}}$, then $f(x)$ is

(1) one-one and onto

(3) many-one and onto

(2) one-one and into

(4) many-one and into

Ans. (2)

Sol. $f(x) = \frac{2^{2x} - 1}{2^{2x} + 1} = \frac{2^{2x} + 1 - 2}{2^{2x} + 1} = 1 - \frac{2}{2^{2x} + 1}$

2^{2x} is one-one so $f(x)$ is one-one

For $x \in (-\infty, \infty)$

$$2^x \in (0, \infty)$$

$$2^{2x} + 1 \in (1, \infty)$$

$$\frac{1}{2^{2x} + 1} \in (0, 1)$$

$$\frac{-2}{2^{2x} + 1} \in (-2, 0)$$

$$1 - \frac{2}{2^{2x} + 1} \in (-1, 1)$$

Range of $f(x)$ is $(-1, 1)$ but codomain of $f(x)$ is $(-\infty, 1)$ so $f(x)$ is into.

15. Given $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ is a hyperbola with latus rectum $12\sqrt{5}$ and eccentricity $\sqrt{\frac{5}{2}}$ and another hyperbola

$\frac{x^2}{A^2} - \frac{y^2}{B^2} = -1$ with latus rectum $15\sqrt{2}$. If the product of transverse axis of both the hyperbola is $100\sqrt{10}$, eccentricity of the later hyperbola is:

(1) 0

(2) 2

(3) $\sqrt{\frac{13}{5}}$

(4) $\sqrt{\frac{11}{5}}$

Ans. (4)

Sol. $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$

$$\frac{2b^2}{a} = 12\sqrt{5} \quad \dots\dots\dots (i)$$

$$\sqrt{1 + \frac{b^2}{a^2}} = \sqrt{\frac{5}{2}} \quad \dots\dots\dots (ii)$$

from (i) and (ii)

$$a = 4\sqrt{5} \text{ and } b^2 = 120$$

$$\frac{x^2}{A^2} - \frac{y^2}{B^2} = -1$$

$$\frac{2A^2}{B} = 15\sqrt{2} \quad \dots\dots\dots (iii)$$

(since product of transverse axis = $100\sqrt{10}$)

$$(2a).(2B) = 100\sqrt{10} \quad \dots\dots\dots (iv)$$

from (iii) & (iv)

$$A^2 = \frac{375}{4} \text{ and } B^2 = \frac{625}{8}$$

$$e_2 = \sqrt{1 + \frac{A^2}{B^2}} = \sqrt{\frac{11}{5}} \text{ (substituting the value of } A^2 \text{ and } B^2 \text{ from the above equation).}$$

